

Image/Video Based 3D Modeling, Rendering, and Registration for Virtual Reality

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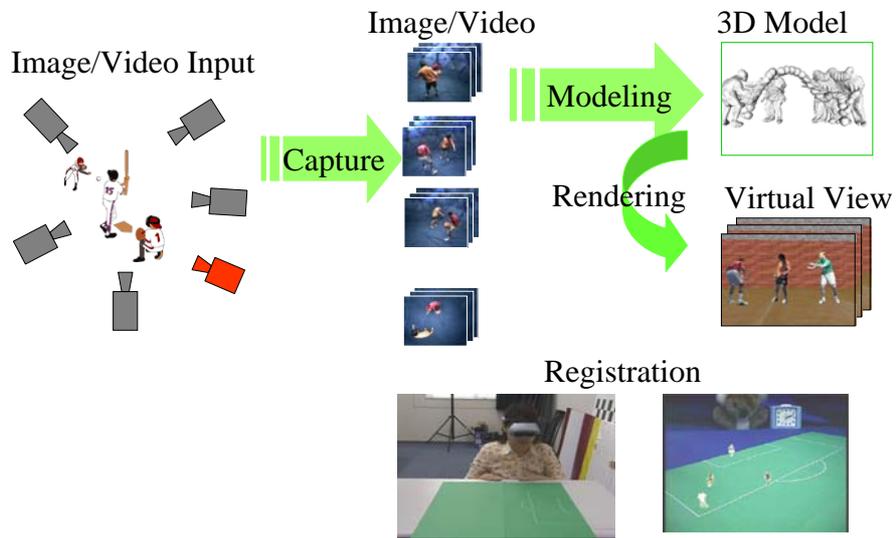
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Contents of this tutorial

- Introduction
- Capturing Image
 - Camera Geometry
 - Calibration
- Modeling and Rendering from Multiple Images
 - Modeling and Rendering from Image Sequences
 - Modeling and Rendering from Multiple Cameras
- Registration
 - Application of Registration to Augmented Reality

Image/Video Based ...



Modeling and Rendering

Example:
3-Man Basketball
(CMU, 1998)

(These are movies.)

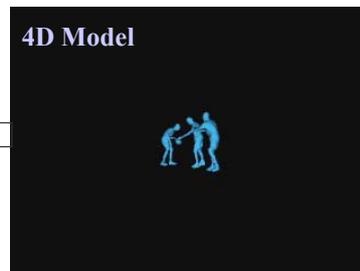
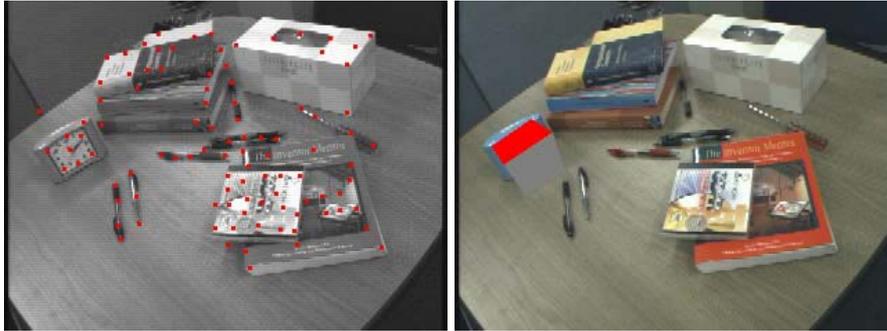


Image Based Registration Example



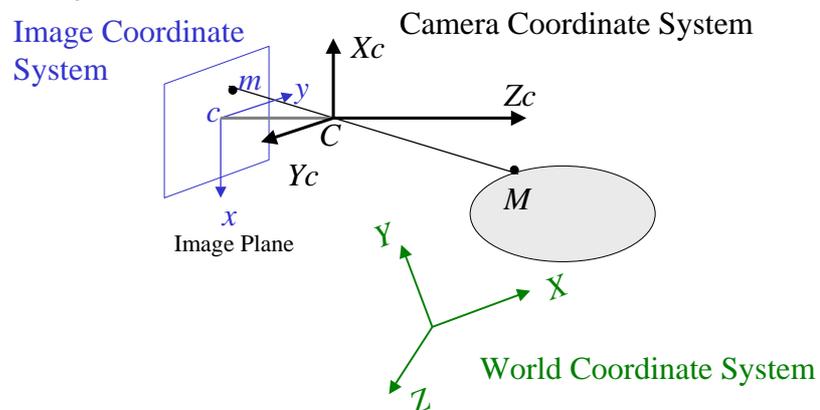
Base Technologies

- Capturing Image
 - Camera Geometry, Calibration
- Modeling and Rendering
 - Shape Recovery
 - Volume Reconstruction
 - Surface Extraction
- Registration
 - Camera Calibration
 - Tracking

Capturing Image

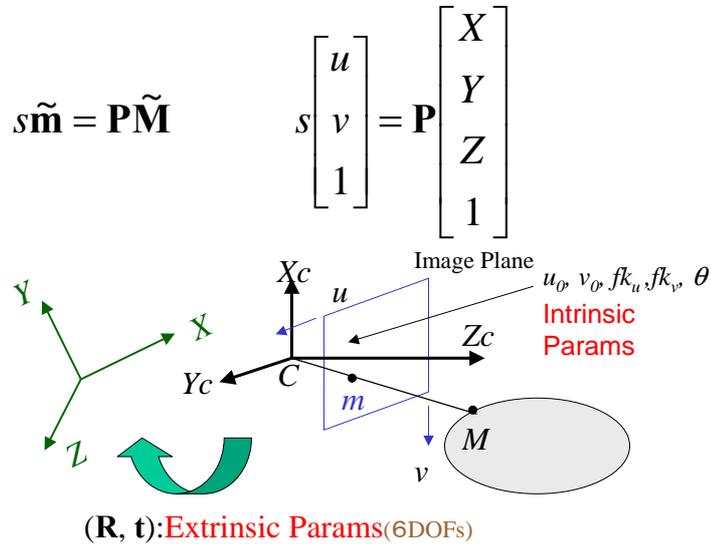
Camera Geometry

- Image: Projection of 3D World onto 2D Plane
 - How the projected position is determined ?
 - Relationship between world coordinate, camera coordinate, and image coordinate



Summary of Projection Matrix

- Projection \mathbf{P} : from World Coord. \mathbf{M} to Image Coord. \mathbf{m}



Camera Calibration

- Intrinsic Parameters (5DOFs)
- Extrinsic Parameters (6DOFs)

Basic Method for Camera Calibration

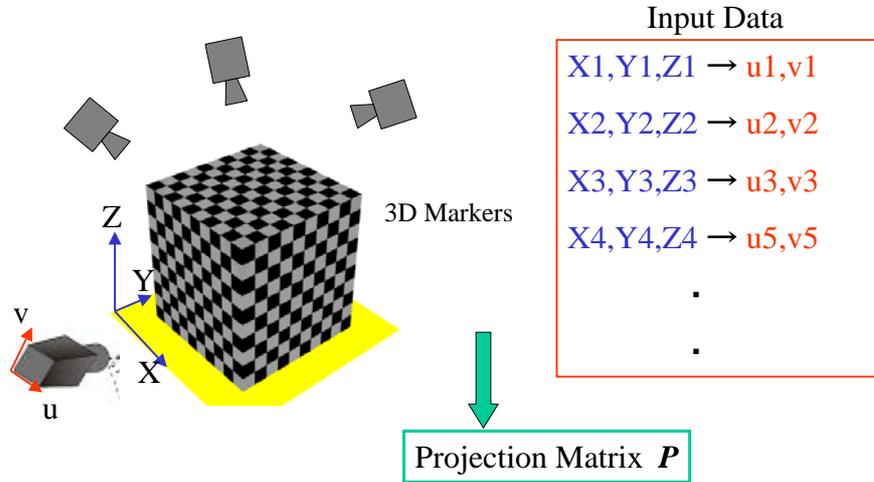
Distribute markers with known 3D positions (X, Y, Z) in objective space

Find image positions (u, v) onto which the markers are projected

$$s\tilde{\mathbf{m}} = \mathbf{P}\tilde{\mathbf{M}}$$

$$s \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \mathbf{P} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

Camera Calibration



Linear Solution for Estimating P

$$s\tilde{\mathbf{m}} = \mathbf{P}\tilde{\mathbf{M}} \quad s \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} P_{11} & P_{12} & P_{13} & P_{14} \\ P_{21} & P_{22} & P_{23} & P_{24} \\ P_{31} & P_{32} & P_{33} & P_{34} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

$(X_n, Y_n, Z_n) \dots (u_n, v_n)$

$$P_{11}X_n + P_{12}Y_n + P_{13}Z_n + P_{14} - P_{31}X_nu_n - P_{32}Y_nu_n - P_{33}Z_nu_n - P_{34}u_n = 0$$

$$P_{21}X_n + P_{22}Y_n + P_{23}Z_n + P_{24} - P_{31}X_nv_n - P_{32}Y_nv_n - P_{33}Z_nv_n - P_{34}v_n = 0$$

$$\begin{matrix} \leftarrow 11 \rightarrow \\ \begin{matrix} \uparrow 2n \\ \begin{bmatrix} X_1 & Y_1 & Z_1 & 1 & 0 & 0 & 0 & 0 & -X_1u_1 & -Y_1u_1 & Z_1u_1 \\ 0 & 0 & 0 & 0 & X_1 & Y_1 & Z_1 & 1 & -X_1v_1 & -Y_1v_1 & Z_1v_1 \\ & & & & & & & & \dots & & \\ X_n & Y_n & Z_n & 1 & 0 & 0 & 0 & 0 & -X_nu_n & -Y_nu_n & Z_nu_n \\ 0 & 0 & 0 & 0 & X_n & Y_n & Z_n & 1 & -X_nv_n & -Y_nv_n & Z_nv_n \end{bmatrix} \begin{bmatrix} P_{11} \\ P_{12} \\ \vdots \\ P_{32} \\ P_{33} \end{bmatrix} = \begin{bmatrix} P_{34}u_1 \\ P_{34}v_1 \\ \vdots \\ P_{34}u_n \\ P_{34}v_n \end{bmatrix} \\ \downarrow 11 \end{matrix} \end{matrix} \quad \downarrow 11$$

$n > 11/2$ markers are required for estimating P

Method for extracting intrinsic and extrinsic parameters from projection matrix \mathbf{P}

$$\mathbf{P} = \mathbf{A}[\mathbf{R}, \mathbf{t}] = \begin{bmatrix} \alpha_u & -\alpha_u \cot \theta & u_0 \\ 0 & \alpha_v / \sin \theta & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} R_{11} & R_{21} & R_{31} & t_x \\ R_{12} & R_{22} & R_{32} & t_y \\ R_{13} & R_{23} & R_{33} & t_z \end{bmatrix}$$

Projection Matrix $\mathbf{P} \rightarrow$ Intrinsic Matrix \mathbf{A}
Extrinsic Matrix and Vector \mathbf{R}, \mathbf{t}

$$\mathbf{P}_w = \begin{bmatrix} P_{11} & P_{12} & P_{13} & P_{14} \\ P_{21} & P_{22} & P_{23} & P_{24} \\ P_{31} & P_{32} & P_{33} & P_{34} \end{bmatrix} = \begin{bmatrix} \mathbf{a}_1 \\ \mathbf{a}_2 \\ \mathbf{a}_3 \end{bmatrix} \mathbf{b} \quad \quad \quad [\mathbf{R}, \mathbf{t}] = \begin{bmatrix} R_{11} & R_{21} & R_{31} & t_x \\ R_{12} & R_{22} & R_{32} & t_y \\ R_{13} & R_{23} & R_{33} & t_z \end{bmatrix} = \begin{bmatrix} \mathbf{r}_1 \\ \mathbf{r}_2 \\ \mathbf{r}_3 \end{bmatrix} \mathbf{t}$$

Property of Rotation Matrix

$$\begin{aligned} |\mathbf{r}_1| = |\mathbf{r}_2| = |\mathbf{r}_3| = 1 \quad \mathbf{r}_1 \bullet \mathbf{r}_2 = 0 \quad \mathbf{r}_2 \bullet \mathbf{r}_3 = 0 \quad \mathbf{r}_3 \bullet \mathbf{r}_1 = 0 \\ \mathbf{r}_1 \times \mathbf{r}_2 = \mathbf{r}_3 \quad \mathbf{r}_2 \times \mathbf{r}_3 = \mathbf{r}_1 \quad \mathbf{r}_3 \times \mathbf{r}_1 = \mathbf{r}_2 \end{aligned}$$

The property of rotation matrix provide the following solution.

$$\mathbf{r}_3 = \frac{\mathbf{a}_3}{|\mathbf{a}_3|} \quad \mathbf{r}_1 = \frac{1}{|\mathbf{a}_2 \times \mathbf{a}_3|} (\mathbf{a}_2 \times \mathbf{a}_3) \quad \mathbf{r}_2 = \mathbf{r}_3 \times \mathbf{r}_1$$

Intrinsic parameter matrix \mathbf{A} can be obtained as

$$\begin{aligned} \cos \theta &= -\frac{(\mathbf{a}_1 \times \mathbf{a}_3) \bullet (\mathbf{a}_2 \times \mathbf{a}_3)}{|\mathbf{a}_1 \times \mathbf{a}_3| |\mathbf{a}_2 \times \mathbf{a}_3|} \\ \alpha_u &= \frac{|\mathbf{a}_1 \times \mathbf{a}_3|}{|\mathbf{a}_3|^2} \sin \theta, \quad \alpha_v = \frac{|\mathbf{a}_2 \times \mathbf{a}_3|}{|\mathbf{a}_3|^2} \sin \theta \end{aligned}$$

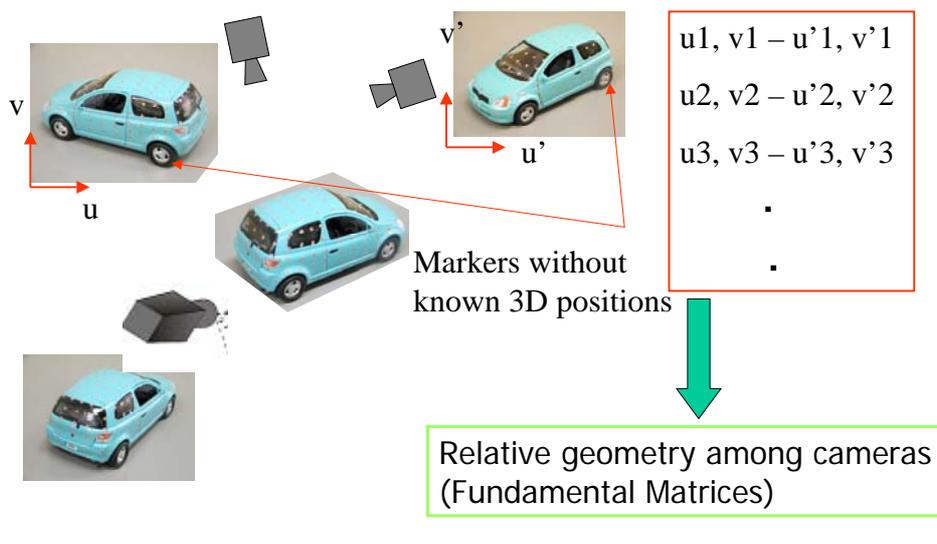
Self Calibration

- Camera calibration without markers

C. Matsunaga and K. Kanatani, "Calibration of a moving camera using a planar pattern: Optimal computation, reliability evaluation and stabilization by the geometric AIC," *Electronics and Communications in Japan, Part 3: Fundamental Electronic Science*, Vol. 84, No. 7 pp. 12-21, 2001.

M. Pollefeys, R. Koch, and L. V. Gool, "Self-Calibration and Metric Reconstruction in spite of Varying and Unknown Internal Camera Parameters," *International Journal of Computer Vision*, 32(1), pp. 7-25, 1999.

Weak Calibration

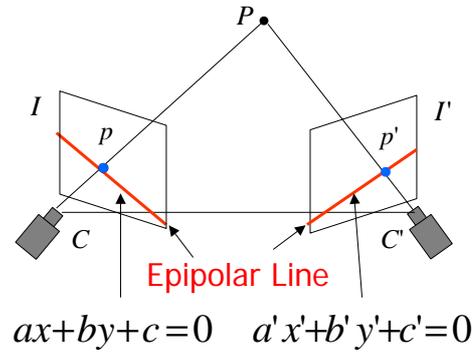


Fundamental Matrix

$$\begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} f_{11} & f_{12} & f_{13} \\ f_{21} & f_{22} & f_{23} \\ f_{31} & f_{32} & f_{33} \end{pmatrix} \begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix}$$

$$= \mathbf{F} \begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} a' \\ b' \\ c' \end{pmatrix} = \mathbf{F}^T \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$$



$$\begin{pmatrix} a \\ b \\ c \end{pmatrix} = \mathbf{F} \begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix}, \quad \begin{pmatrix} a' \\ b' \\ c' \end{pmatrix} = \mathbf{F}^T \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}, \quad (x, y, 1) \mathbf{F} \begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix} = 0$$

One corresponding point gives the following equation.

$$x(x'F_{11} + y'F_{12} + F_{13}) + y(x'F_{21} + y'F_{22} + F_{23}) + (x'F_{31} + y'F_{32} + F_{33}) = 0$$

n corresponding points

$$\begin{bmatrix} x_1x_1' & x_1y_1' & x_1 & y_1x_1' & y_1y_1' & y_1 & x_1' & y_1' \\ x_2x_2' & x_2y_2' & x_2 & y_2x_2' & y_2y_2' & y_2 & x_2' & y_2' \\ \vdots & \vdots \\ x_nx_n' & x_ny_n' & x_n & y_nx_n' & y_ny_n' & y_n & x_n' & y_n' \end{bmatrix} \begin{bmatrix} F_{11} \\ F_{12} \\ F_{13} \\ F_{21} \\ F_{22} \\ F_{23} \\ F_{31} \\ F_{32} \end{bmatrix} = - \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$

$$F_{33} = 1$$

Strong/Weak Calibration

	Strong Calibration	Weak Calibration
To be estimated	Projection Matrix $s \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \mathbf{P} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$	Fundamental Matrix $\begin{bmatrix} a_1 \\ b_1 \\ 1 \end{bmatrix} = \mathbf{F} \begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix}$
Required data	3D Space – 2D Image Correspondences (Artificial Markers required)	2D Image – 2D Image Correspondences (Natural features)
Size Shape	Available	Unknown (Ambiguity in Projective Transform)

Plane-Based Calibration

A Flexible New Technique for Camera Calibration

<http://research.microsoft.com/~zhang/calib/>



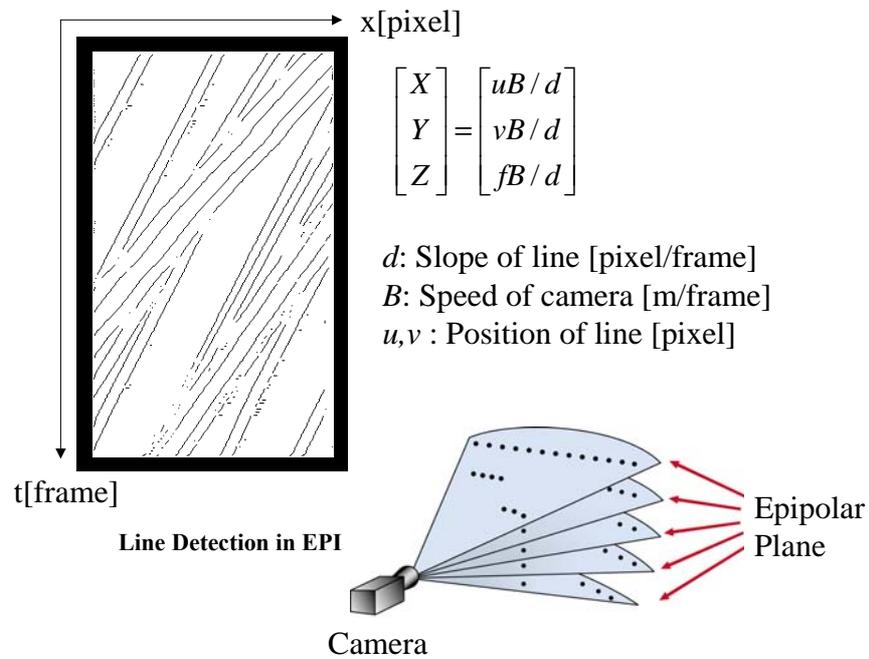
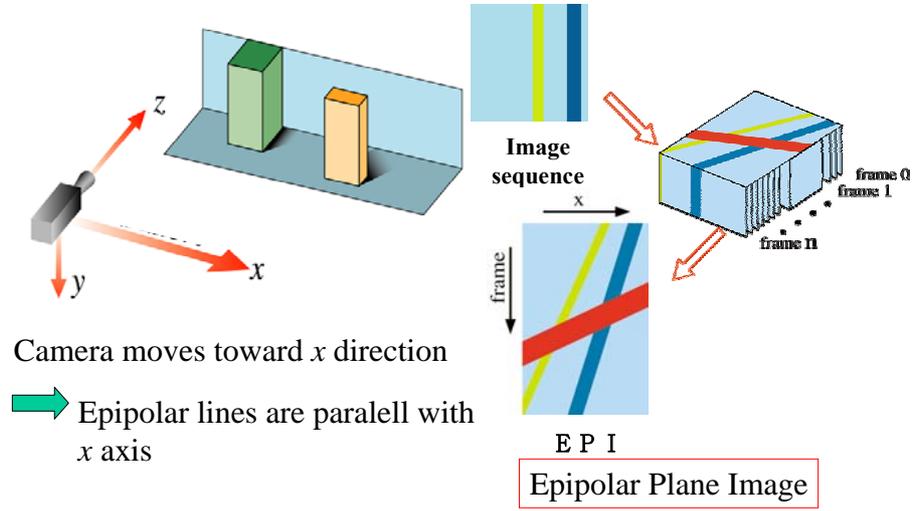
Multiple Images of Checker Pattern Board at Arbitrary Pose

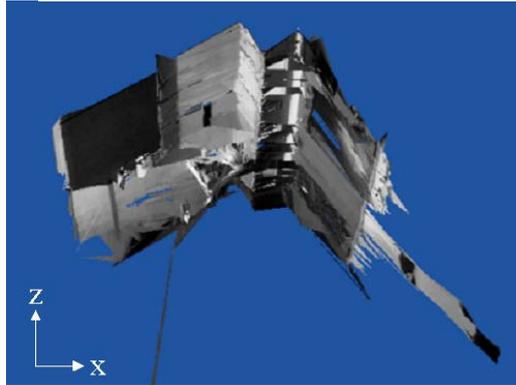
Modeling and Rendering

Modeling and Rendering

- Image Sequence captured by a camera
 - Motion Stereo
 - Feature point tracking
 - Reflectance analysis
- Multiple Cameras
 - Silhouette Intersection
 - Merge Stereo
 - Space Carving/Voxel Coloring

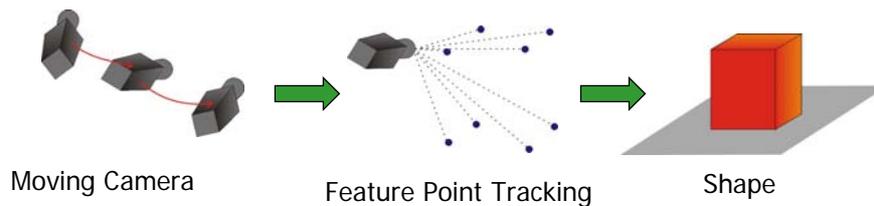
Motion Stereo



120th frame240th frame360th frameRecovered Shape with
Texture of Input Images

Feature point tracking

- Feature points are tracked.
- Positions of tracked feature points are used for shape modeling.
- Standard feature tracking algorithm
 - **Kanade-Lucas-Tomasi Feature Tracker**
(<http://robotics.stanford.edu/~birch/klt/>)



Moving Camera

Feature Point Tracking

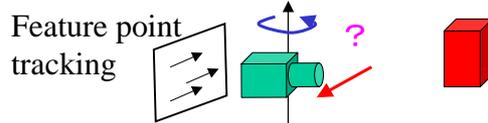
Shape

Factorization

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C. Tomasi and T. Kanade, Shape and Motion from Image Streams under Orthography: a Factorization Method, International Journal of Computer Vision, 9:2, 137-154, 1992

- Estimation of motion of perspective camera
 - Difficult to distinguish translation and rotation



- Depth variation of object shape is relatively smaller than distance to the object.



Orthographic assumption of camera

- Easy to distinguish translation and rotation
- Shift of feature points can be segmented into camera motion and object shape via linear computation.

Factorization: measurement matrix

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$$\tilde{W} = \begin{bmatrix} \tilde{u}_{11} & \cdots & \tilde{u}_{1P} \\ \vdots & \tilde{u}_{fP} & \vdots \\ \tilde{u}_{F1} & \cdots & \tilde{u}_{FP} \\ \tilde{v}_{11} & \cdots & \tilde{v}_{1P} \\ \vdots & \tilde{v}_{fP} & \vdots \\ \tilde{v}_{F1} & \cdots & \tilde{v}_{FP} \end{bmatrix}$$

P (number of feature points)

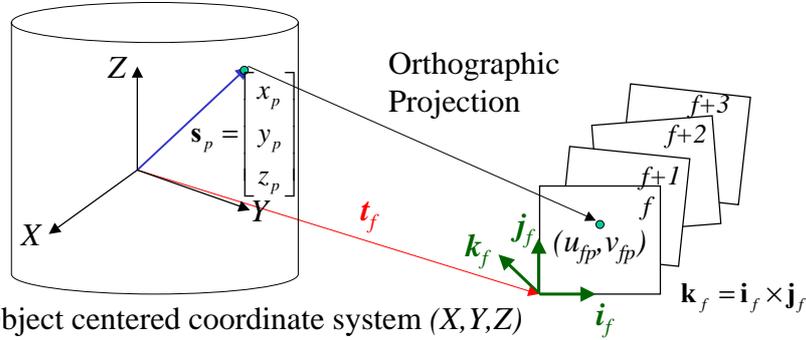
F (number of frames)

F (number of frames)

$$\tilde{u}_{fp} = u_{fp} - a_f \quad a_f = \frac{1}{P} \sum_{p=1}^P u_{fp}$$

$$\tilde{v}_{fp} = v_{fp} - b_f \quad b_f = \frac{1}{P} \sum_{p=1}^P v_{fp}$$

Shape and Motion under Orthographic Projection



Object centered coordinate system (X,Y,Z)

$$\tilde{u}_{fp} = u_{fp} - a_f$$

$$u_{fp} = \mathbf{i}_f^T (\mathbf{s}_p - \mathbf{t}_f) = \mathbf{i}_f^T (\mathbf{s}_p - \mathbf{t}_f) - \frac{1}{P} \sum_{q=1}^P \mathbf{i}_f^T (\mathbf{s}_q - \mathbf{t}_f)$$

$$v_{fp} = \mathbf{j}_f^T (\mathbf{s}_p - \mathbf{t}_f) = \mathbf{i}_f^T \left(\mathbf{s}_p - \frac{1}{P} \sum_{q=1}^P \mathbf{s}_q \right) = \mathbf{i}_f^T \mathbf{s}_p$$

$$\tilde{u}_{fp} = \mathbf{i}_f^T \mathbf{s}_p$$

$$\tilde{v}_{fp} = \mathbf{j}_f^T \mathbf{s}_p$$

$$\tilde{\mathbf{W}} = \begin{bmatrix} \tilde{u}_{11} & \cdots & \tilde{u}_{1P} \\ \vdots & \tilde{u}_{fp} & \vdots \\ \tilde{u}_{F1} & \cdots & \tilde{u}_{FP} \\ \tilde{v}_{11} & \cdots & \tilde{v}_{1P} \\ \vdots & \tilde{v}_{fp} & \vdots \\ \tilde{v}_{F1} & \cdots & \tilde{v}_{FP} \end{bmatrix} = \begin{bmatrix} \mathbf{i}_1^T \mathbf{s}_1 & \cdots & \mathbf{i}_1^T \mathbf{s}_P \\ \vdots & \mathbf{i}_f^T \mathbf{s}_p & \vdots \\ \mathbf{i}_F^T \mathbf{s}_1 & \cdots & \mathbf{i}_F^T \mathbf{s}_P \\ \mathbf{j}_1^T \mathbf{s}_1 & \cdots & \mathbf{j}_1^T \mathbf{s}_P \\ \vdots & \mathbf{j}_f^T \mathbf{s}_p & \vdots \\ \mathbf{j}_F^T \mathbf{s}_1 & \cdots & \mathbf{j}_F^T \mathbf{s}_P \end{bmatrix} = \begin{bmatrix} \mathbf{i}_1^T \\ \vdots \\ \mathbf{i}_F^T \\ \mathbf{j}_1^T \\ \vdots \\ \mathbf{j}_F^T \end{bmatrix} \begin{bmatrix} \mathbf{s}_1 & \cdots & \mathbf{s}_P \end{bmatrix} = \mathbf{R}\mathbf{S}$$

Camera Rotation Matrix (points to R)
Shape Matrix (points to S)

RANK of $\tilde{\mathbf{W}}$ is 3

Segmentation of Measurement Matrix into Shape and Motion

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$$\tilde{\mathbf{W}} = \mathbf{O}_1 \boldsymbol{\Sigma} \mathbf{O}_2 = \begin{bmatrix} \mathbf{O}_1 & \boldsymbol{\Sigma} & \mathbf{O}_2 \end{bmatrix}$$

$\mathbf{O}_1^T \mathbf{O}_1 = \mathbf{O}_2^T \mathbf{O}_2 = \mathbf{I}$
 $\boldsymbol{\Sigma} = \begin{bmatrix} \sigma_1 & & \mathbf{0} \\ & \ddots & \\ \mathbf{0} & & \sigma_p \end{bmatrix}$
 $\sigma_1, \sigma_2, \dots, \sigma_p$
 Eigen values of $\tilde{\mathbf{W}}$

$$= \begin{bmatrix} \mathbf{O}'_1 & \mathbf{O}''_1 & \boldsymbol{\Sigma}' & \mathbf{0} \\ \mathbf{0} & \boldsymbol{\Sigma}'' & \mathbf{O}'_2 & \mathbf{O}''_2 \end{bmatrix}$$

$\tilde{\mathbf{W}} = \mathbf{O}'_1 \boldsymbol{\Sigma}' \mathbf{O}'_2 + \mathbf{O}''_1 \boldsymbol{\Sigma}'' \mathbf{O}''_2$
RANK of $\tilde{\mathbf{W}}$ is 3 $\Rightarrow \boldsymbol{\Sigma}'' = \mathbf{0}$

$$\hat{\mathbf{W}} = \begin{bmatrix} \mathbf{O}'_1 & \boldsymbol{\Sigma}' & \mathbf{O}'_2 \end{bmatrix} \quad \hat{\mathbf{R}} = \begin{bmatrix} \mathbf{O}'_1 \\ \boldsymbol{\Sigma}'^{1/2} \end{bmatrix} \quad \hat{\mathbf{S}} = \boldsymbol{\Sigma}'^{1/2} \begin{bmatrix} \mathbf{O}'_2 \end{bmatrix}$$

Expected factorization

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$$\tilde{\mathbf{W}} = \begin{bmatrix} \tilde{u}_{11} & \dots & \tilde{u}_{1p} \\ \vdots & \tilde{u}_{fp} & \vdots \\ \tilde{u}_{F1} & \dots & \tilde{u}_{FP} \\ \vdots & \tilde{v}_{fp} & \vdots \\ \tilde{v}_{11} & \dots & \tilde{v}_{1p} \\ \vdots & \tilde{v}_{fp} & \vdots \\ \tilde{v}_{F1} & \dots & \tilde{v}_{FP} \end{bmatrix} = \begin{bmatrix} \mathbf{i}_1^T \mathbf{s}_1 & \dots & \mathbf{i}_1^T \mathbf{s}_p \\ \vdots & \mathbf{i}_f^T \mathbf{s}_p & \vdots \\ \mathbf{i}_F^T \mathbf{s}_1 & \dots & \mathbf{i}_F^T \mathbf{s}_p \\ \vdots & \mathbf{j}_1^T \mathbf{s}_1 & \vdots \\ \vdots & \mathbf{j}_f^T \mathbf{s}_p & \vdots \\ \mathbf{j}_F^T \mathbf{s}_1 & \dots & \mathbf{j}_F^T \mathbf{s}_p \end{bmatrix} = \begin{bmatrix} \mathbf{i}_1^T \\ \vdots \\ \mathbf{i}_F^T \\ \mathbf{j}_1^T \\ \vdots \\ \mathbf{j}_F^T \end{bmatrix} \begin{bmatrix} \mathbf{s}_1 & \dots & \mathbf{s}_p \end{bmatrix} = \mathbf{R} \mathbf{S}$$

Orthogonal

$$\hat{\mathbf{R}} = \begin{bmatrix} \hat{\mathbf{i}}_1^T \\ \vdots \\ \hat{\mathbf{i}}_F^T \\ \hat{\mathbf{j}}_1^T \\ \vdots \\ \hat{\mathbf{j}}_F^T \end{bmatrix}, \quad \hat{\mathbf{S}} = [\hat{\mathbf{s}}_1 \quad \dots \quad \hat{\mathbf{s}}_p]$$

$\mathbf{R} = \hat{\mathbf{R}} \mathbf{Q}$
 $\mathbf{S} = \mathbf{Q}^{-1} \hat{\mathbf{S}}$

$$\begin{aligned} \hat{\mathbf{i}}_f^T \mathbf{Q} \mathbf{Q}^T \hat{\mathbf{i}}_f^T &= 1 \\ \hat{\mathbf{j}}_f^T \mathbf{Q} \mathbf{Q}^T \hat{\mathbf{j}}_f^T &= 1 \\ \hat{\mathbf{i}}_f^T \mathbf{Q} \mathbf{Q}^T \hat{\mathbf{j}}_f^T &= 0 \end{aligned}$$

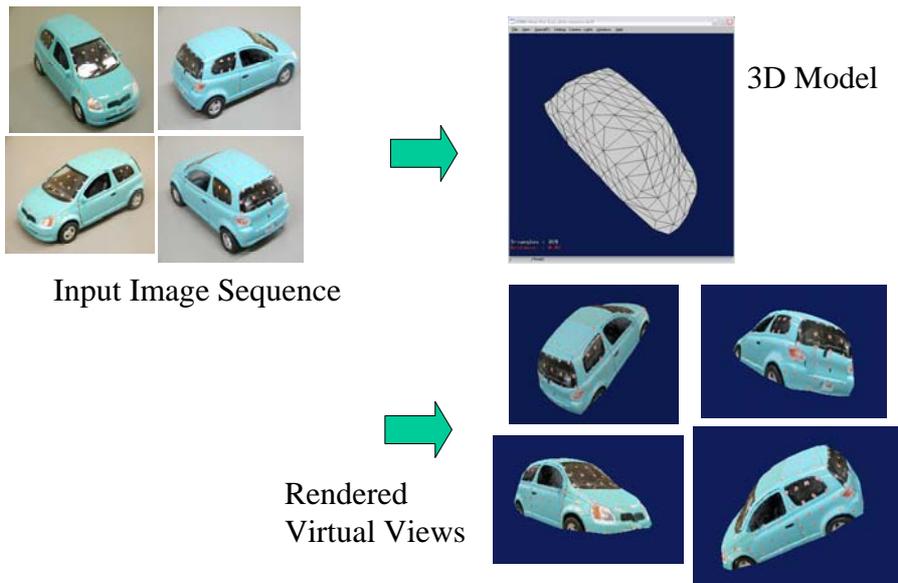
Factorization: Algorithm

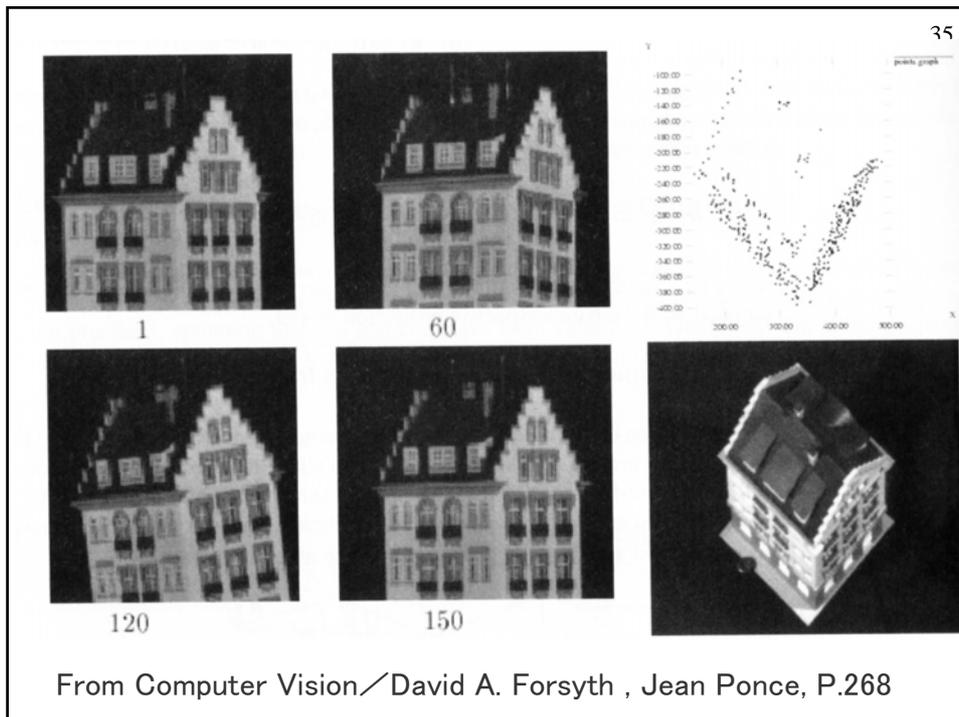
1. Make a measurement matrix $\tilde{\mathbf{W}}$ from tracked feature points.
2. SVD $\tilde{\mathbf{W}}$, then obtain $\mathbf{O}_1 \mathbf{\Sigma} \mathbf{O}_2$ ($\tilde{\mathbf{W}} = \mathbf{O}_1 \mathbf{\Sigma} \mathbf{O}_2$)
3. Extract $\mathbf{O}'_1, \mathbf{\Sigma}', \mathbf{O}'_2$ from $\mathbf{O}_1, \mathbf{\Sigma}, \mathbf{O}_2$
4. Obtain $\hat{\mathbf{R}} = \mathbf{O}'_1 [\mathbf{\Sigma}']^{1/2}$, $\hat{\mathbf{S}} = [\mathbf{\Sigma}']^{1/2} \mathbf{O}'_2$
5. Determine \mathbf{Q} from the orthogonal condition of $\hat{\mathbf{R}}$

$$\hat{\mathbf{i}}_f^T \mathbf{Q} \mathbf{Q}^T \hat{\mathbf{i}}_f = 1, \hat{\mathbf{j}}_f^T \mathbf{Q} \mathbf{Q}^T \hat{\mathbf{j}}_f = 1, \hat{\mathbf{i}}_f^T \mathbf{Q} \mathbf{Q}^T \hat{\mathbf{j}}_f = 0$$
6. Determine \mathbf{R} and \mathbf{S} according to

$$\mathbf{R} = \hat{\mathbf{R}} \mathbf{Q}, \quad \mathbf{S} = \mathbf{Q}^{-1} \hat{\mathbf{S}}$$

Modeled Shape via Factorization





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Shape Modeling from Reflectance Analysis

What determines image intensity is

- Surface Material ρ
- Surface Orientation \mathbf{n}
- Light Source Direction \mathbf{S}
- Viewpoint Direction \dots

Diffuse reflectance surface (Lambertian surface)

↳ Independent from Viewpoint Direction

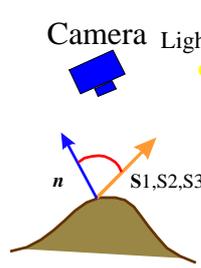
$$L = \rho \cos\theta = \rho(\mathbf{S} \cdot \mathbf{n})$$

Photometric Stereo

Three images are captured under three different light source directions ($\mathbf{S}_1, \mathbf{S}_2, \mathbf{S}_3$)

$$L = \rho \cos \theta_s$$

$$= \rho(\mathbf{S} \cdot \mathbf{n})$$



$$\begin{bmatrix} L_1 \\ L_2 \\ L_3 \end{bmatrix} = \rho \begin{bmatrix} (\mathbf{S}_1 \cdot \mathbf{n}) \\ (\mathbf{S}_2 \cdot \mathbf{n}) \\ (\mathbf{S}_3 \cdot \mathbf{n}) \end{bmatrix} = \rho \begin{bmatrix} \mathbf{S}_1^T \\ \mathbf{S}_2^T \\ \mathbf{S}_3^T \end{bmatrix} \mathbf{n}$$

$$\mathbf{L} = \rho \mathbf{S} \mathbf{n}$$

$$\mathbf{n} = \frac{\mathbf{S}^{-1} \mathbf{L}}{\rho}$$

$$\rho = |\mathbf{S}^{-1} \mathbf{L}|$$

$$= \rho \begin{bmatrix} S_{1x} & S_{1y} & S_{1z} \\ S_{2x} & S_{2y} & S_{2z} \\ S_{3x} & S_{3y} & S_{3z} \end{bmatrix} \begin{bmatrix} n_x \\ n_y \\ n_z \end{bmatrix}$$

Shape Recovery from Surface Normal \mathbf{n}

Orthographics Projection Camera



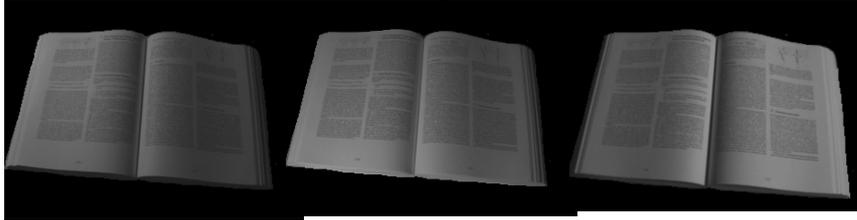
(x, y) in image is coincide with (X, Y) in 3D space

Integration (Summation) of $\mathbf{n}(x, y) \Rightarrow$ Shape $z(x, y)$

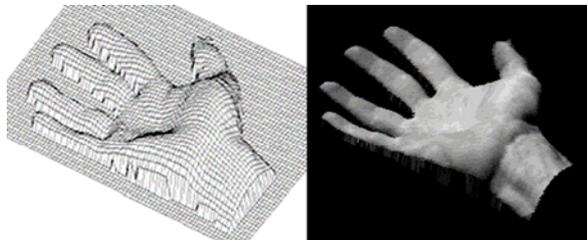
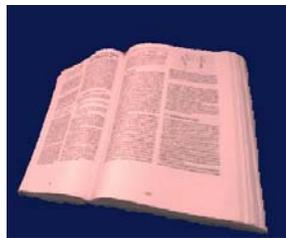
Shape $Z(x, y, z(x, y))$ and Surface Normal $\mathbf{n}(x, y)$

$$\mathbf{n}(x, y) = \frac{1}{\sqrt{\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2 + 1}} \begin{bmatrix} -\frac{\partial z}{\partial x} \\ -\frac{\partial z}{\partial y} \\ 1 \end{bmatrix}$$

Example



3D Shape



Reinhard Klette, Ryszard Kozera, and Karsten Schlüns, Shape from Shading and Photometric Stereo Methods, CITR-TR-20, May 1998

Computer Science Department of The University of Auckland, CITR at Tamaki Campus (<http://www.tcs.auckland.ac.nz>)

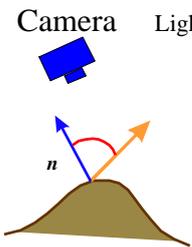
Photometric Stereo with N Light Sources

41

$$L = \rho \cos \theta_s$$

$$= \rho(\mathbf{S} \cdot \mathbf{n})$$

$$\begin{bmatrix} L_1 \\ L_2 \\ \vdots \\ L_N \end{bmatrix} = \rho \begin{bmatrix} (\mathbf{S}_1 \cdot \mathbf{n}) \\ (\mathbf{S}_2 \cdot \mathbf{n}) \\ \vdots \\ (\mathbf{S}_N \cdot \mathbf{n}) \end{bmatrix} = \rho \begin{bmatrix} \mathbf{S}_1^T \\ \mathbf{S}_2^T \\ \vdots \\ \mathbf{S}_N^T \end{bmatrix} \mathbf{n}$$



Camera Light Source

$$= \rho \begin{bmatrix} S_{1x} & S_{1y} & S_{1z} \\ S_{2x} & S_{2y} & S_{2z} \\ \vdots & \vdots & \vdots \\ S_{Nx} & S_{Ny} & S_{Nz} \end{bmatrix} \begin{bmatrix} n_x \\ n_y \\ n_z \end{bmatrix}$$

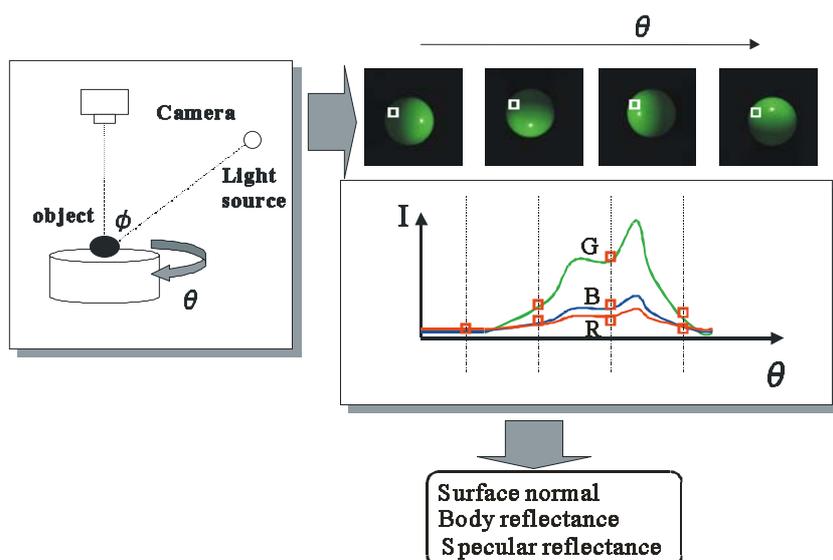
$$\mathbf{L} = \rho \mathbf{S} \mathbf{n}$$

$$\mathbf{n} = \frac{\mathbf{S}^{-1} \mathbf{L}}{\rho}$$

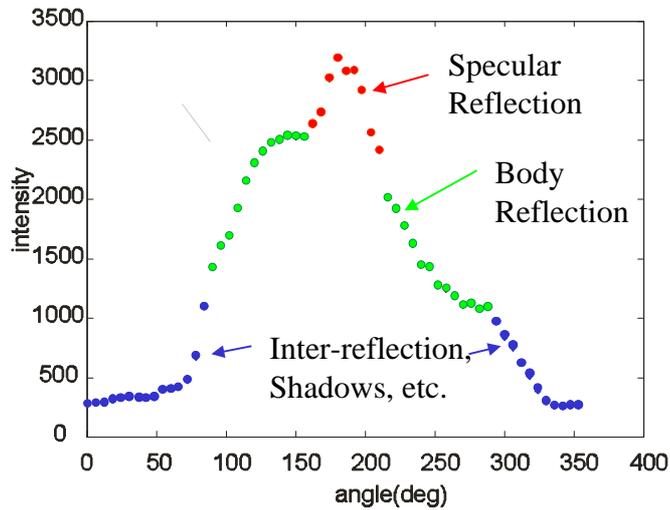
$$\rho = |\mathbf{S}^{-1} \mathbf{L}|$$

Shape Modeling from Reflectance Analysis

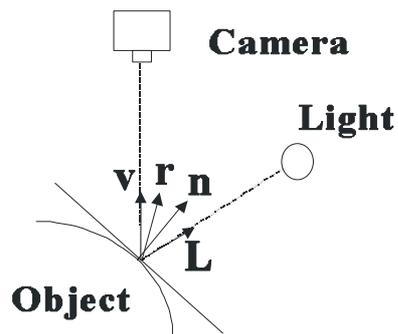
42



Example of Intensity Curve



Phong's Reflectance Model



$$I = d(\mathbf{L} \cdot \mathbf{n}) + s(\mathbf{r} \cdot \mathbf{v})^k$$

d : body reflectance

s : specular reflectance

k : specular sharpness

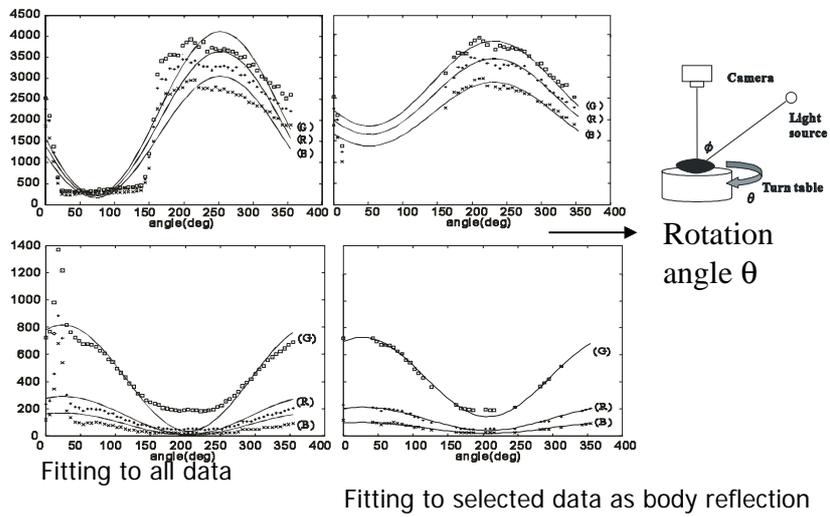
\mathbf{n} : surface normal

\mathbf{L} : light source direction

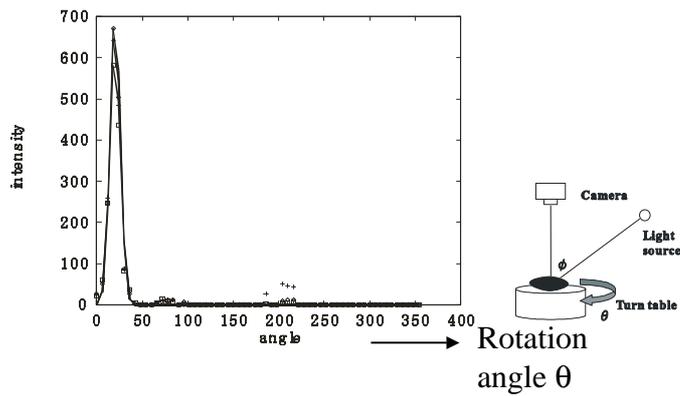
\mathbf{v} : camera direction

$$\mathbf{r} = (2\mathbf{n} - \mathbf{L}) / (|\mathbf{L} - \mathbf{n}|)$$

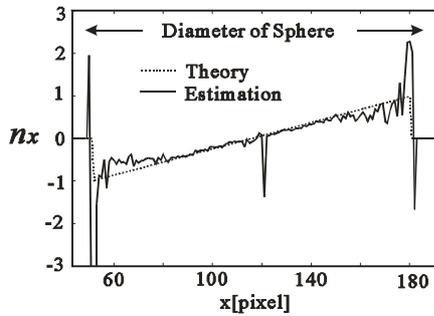
Fitting to body reflection



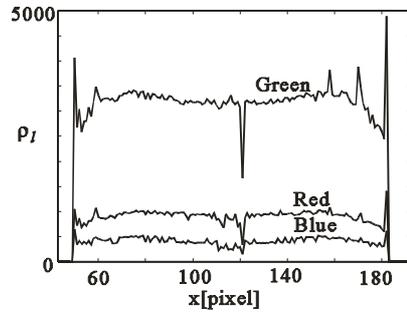
Fitting to specular reflection



Results for Sphere



Comparison of estimated surfaced normal with theoretical value

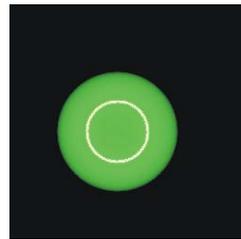


Estimated body reflectance

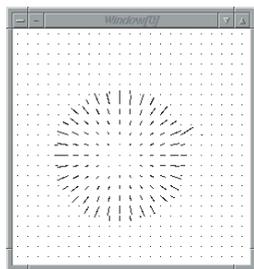
Results for Sphere



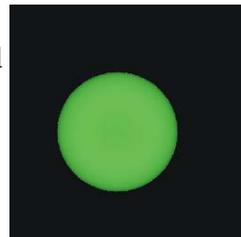
Example of input image



Recovered body reflectance from all intensity data

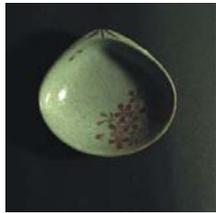


Recovered needle map

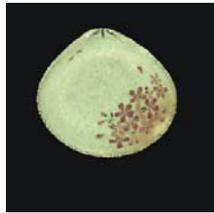


Recovered body reflectance from selected intensity data

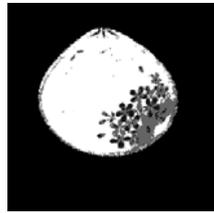
Shape and Reflectance



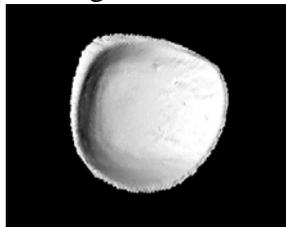
Example of input image



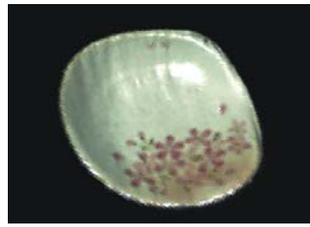
Body reflectance



Specular reflectance



3D Shape

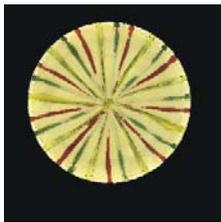


Rendered image at virtual view

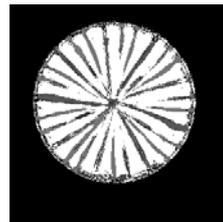
Shape and Reflectance



Example of input image



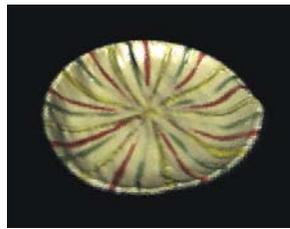
Body reflectance



Specular reflectance



3D Shape



Rendered image at virtual view

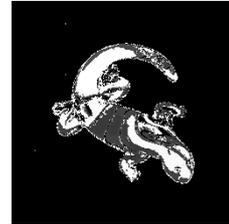
Shape and Reflectance



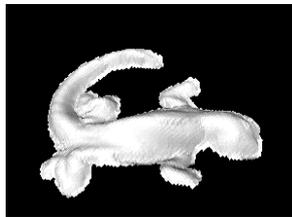
Example of
input image



Body reflectance



Specular reflectance

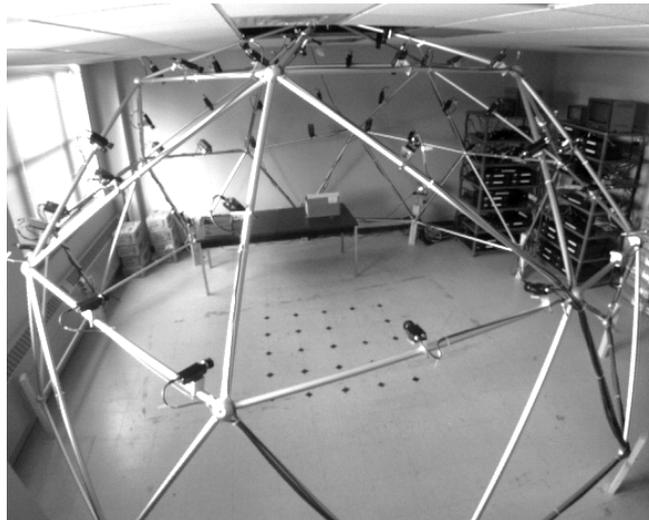


3D Shape



Rendered image at virtual view

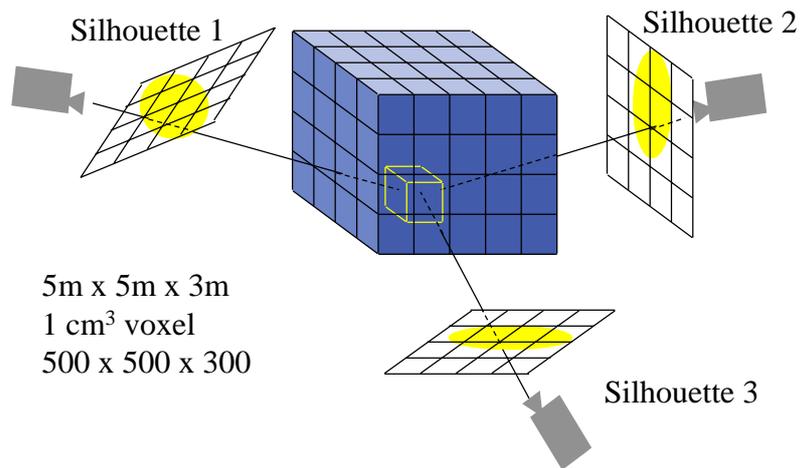
Modeling and Rendering via Multiple Cameras⁵²



Virtualized Reality: Dome with 51 Cameras in CMU

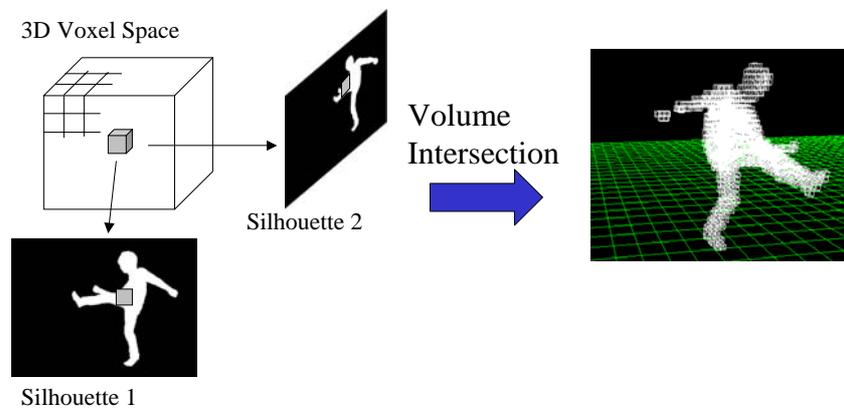
Silhouette Intersection

$$F(X, Y, Z) = \begin{cases} 1; & \text{if all the projected points are included in the silhouette} \\ 0; & \text{otherwise} \end{cases}$$



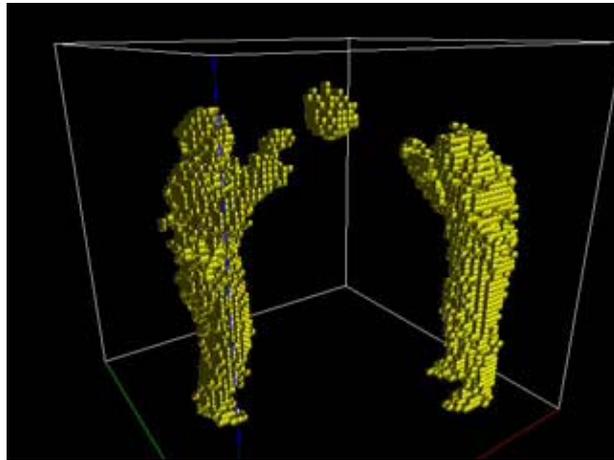
Silhouette Intersection

– Simple, but impossible to recover concaved shape



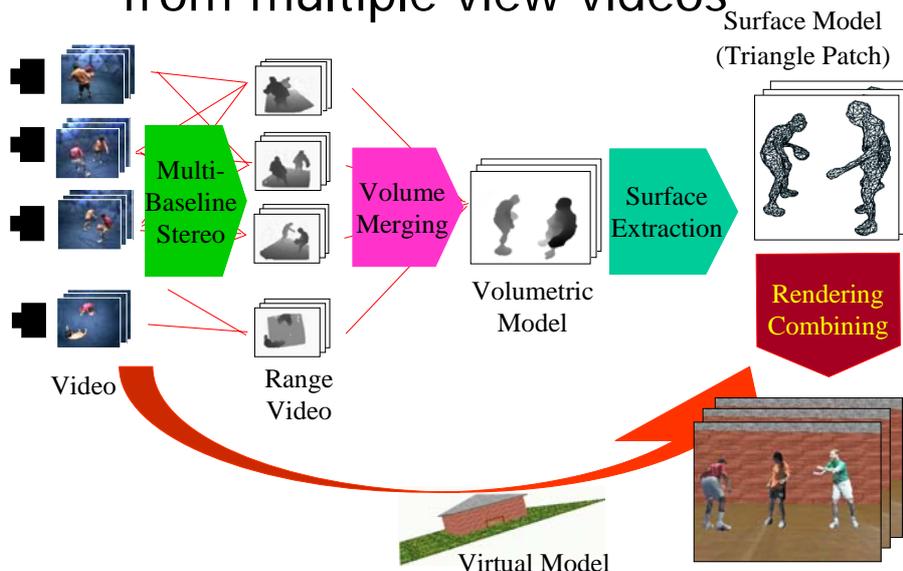
Example of Silhouette Intersection

55

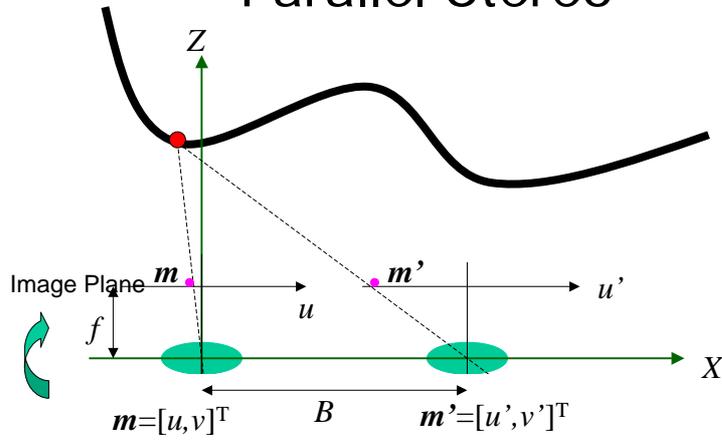


Modeling and Rendering from multiple view videos

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Parallel Stereo

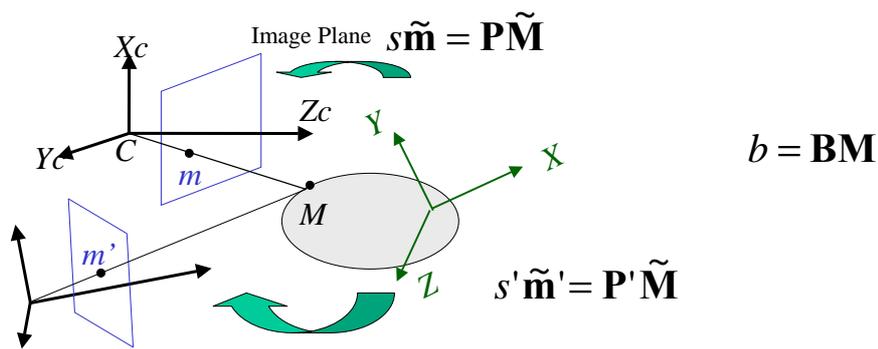


Disparity: $d = u - u'$

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} uB/d \\ vB/d \\ fB/d \end{bmatrix}$$

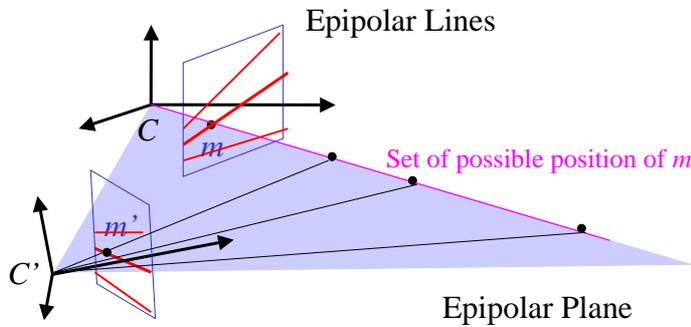
Depth Z is inversely proportional to disparity d.

Non-Parallel Stereo



$$\begin{bmatrix} P_{14} - uP_{34} \\ P_{24} - vP_{34} \\ P'_{14} - u'P'_{34} \\ P'_{24} - v'P'_{34} \end{bmatrix} = \begin{bmatrix} uP_{31} - P_{11} & uP_{32} - P_{12} & uP_{33} - P_{13} \\ vP_{31} - P_{21} & vP_{32} - P_{22} & vP_{33} - P_{23} \\ u'P'_{31} - P'_{11} & u'P'_{32} - P'_{12} & u'P'_{33} - P'_{13} \\ v'P'_{31} - P'_{21} & v'P'_{32} - P'_{22} & v'P'_{33} - P'_{23} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

Epipolar Geometry

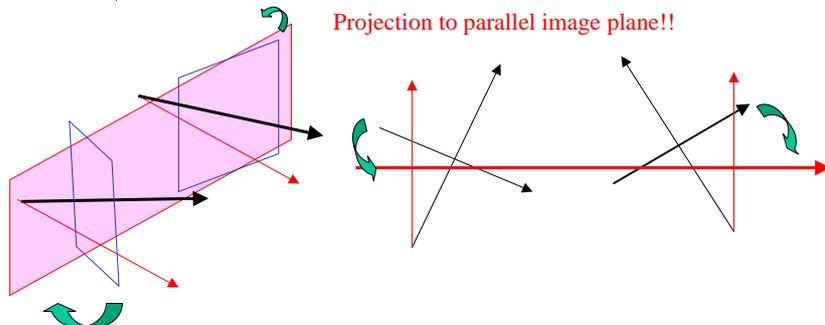


➡ Searching of corresponding point is 1D searching.

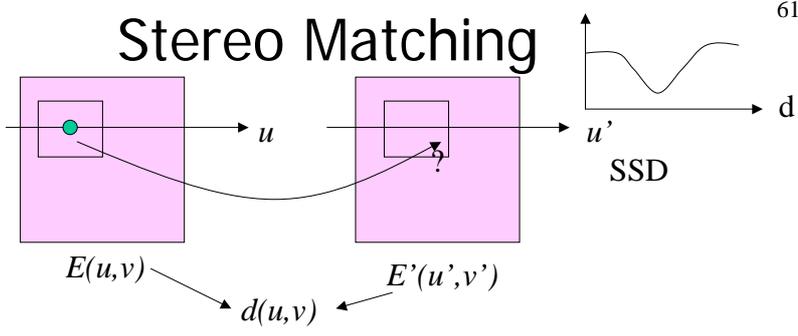
Rectification

- Stereo Correspondence
 - **Parallel Cameras** : Epipolar lines are parallel to u axis.
 - **Non-Parallel Cameras** : Search along epipolar lines
- Convert to image pair captured with parallel cameras

➡ **Rectification**



Stereo Matching

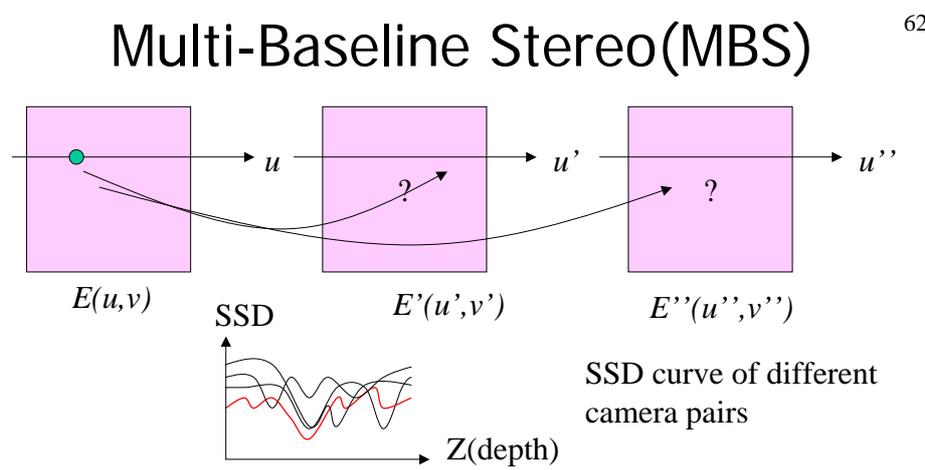


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Pattern matching of small local area

$$SSD = \sum \sum |E(u + d, v) - E'(u', v')|^2$$

Multi-Baseline Stereo(MBS)



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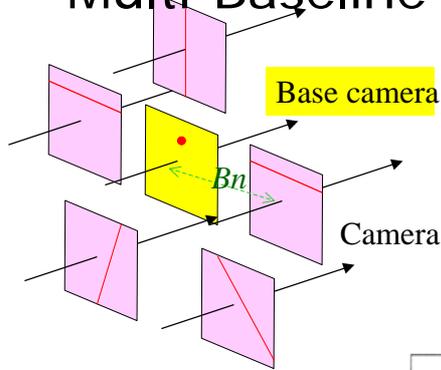
SSD curve of different camera pairs

Integrate all the SSD curve

↓
 Different base-line

Multiple Baseline Stereo:MBS

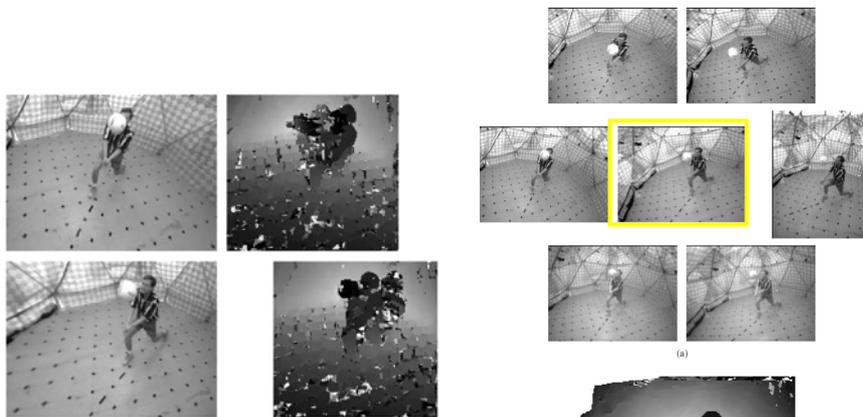
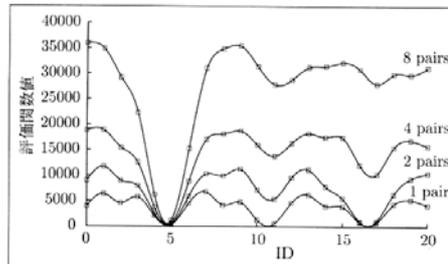
Multi-Baseline Stereo(MBS)



Stereo between camera n and base camera

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} uB_n/d \\ vB_n/d \\ fB_n/d \end{bmatrix}$$

$$\frac{1}{Z} = \frac{d}{fB_n} ; \text{ Inverse Distance(ID)}$$



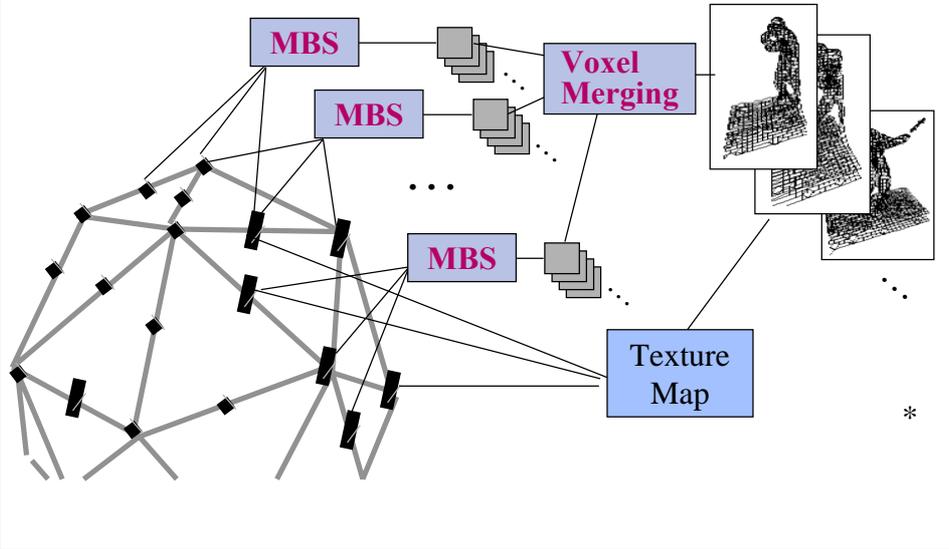
Depth images via two cameras

Up : Depth at left camera.

Dn: Depth at right camera.

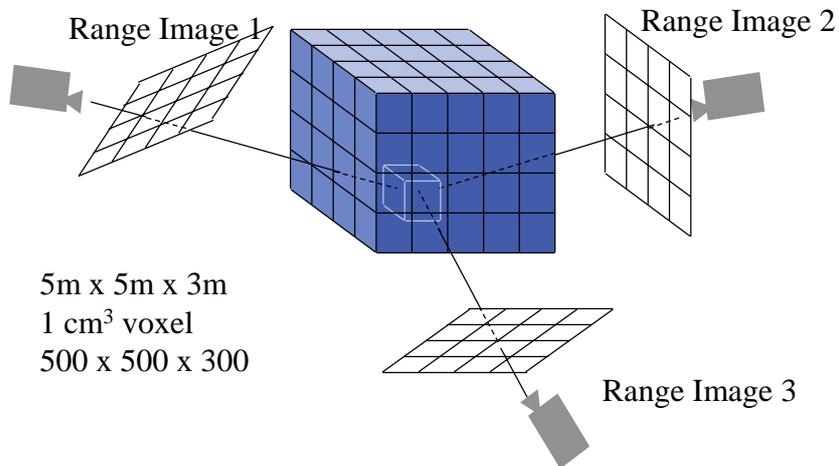
Depth image via 7 cameras

3D Complete Surface Modeling



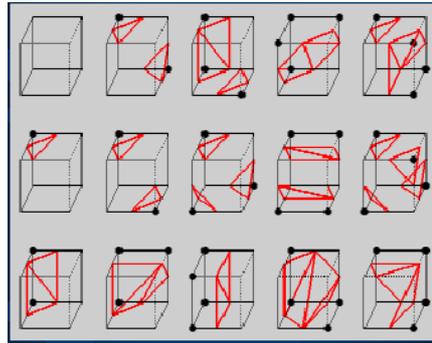
Method for synthesizing range images

Surface representation with implicit function :

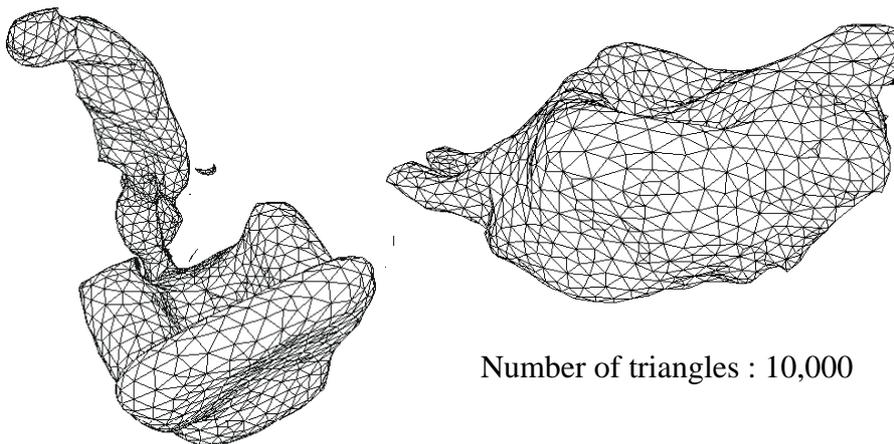
$$F(x,y,z) \begin{cases} > 0 & \text{outside} \\ = 0 & \text{on the surface} \\ < 0 & \text{inside} \end{cases}$$


Surface extraction from the volume

- Set of $F(x,y,z)=0 \rightarrow$ Object surface
- Marching Cubes Algorithm
 - Extract surface voxels: Voxel at which sign of $F(x,y,z)$ changes.
 - Sign pattern around the surface voxel: Mesh pattern
 - Organizing polygon mesh



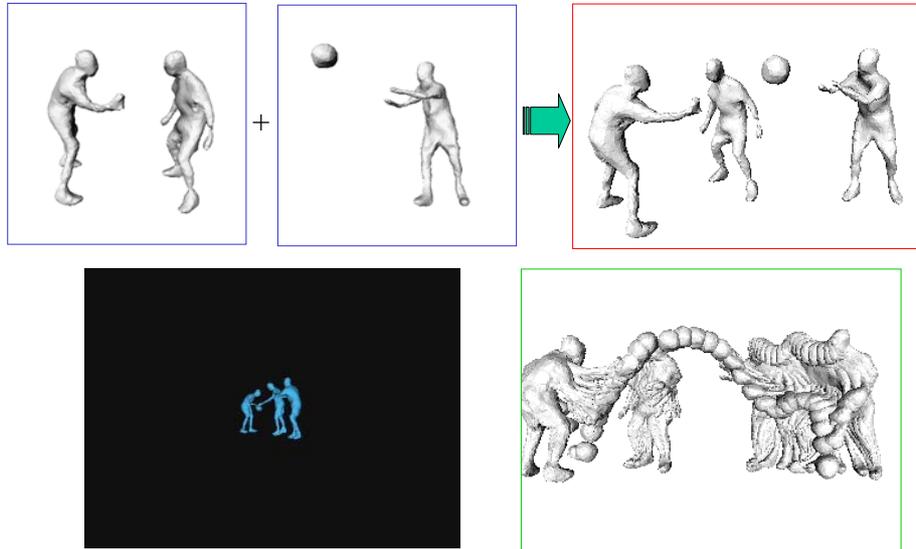
Recovered polygon mesh surface



Example of mesh simplify algorithm

<http://graphics.cs.uiuc.edu/~garland/software/qslim.html>

3D surface mesh with motion



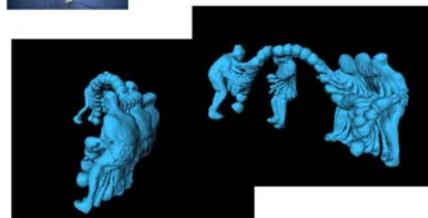
Virtualized Reality : (CMU)



3D Room



The 51-camera video [Vedula, Saito, Kanade et.al.98] sequence are processed to produce a complete 4-dimensional (time + 3D) description of an event.

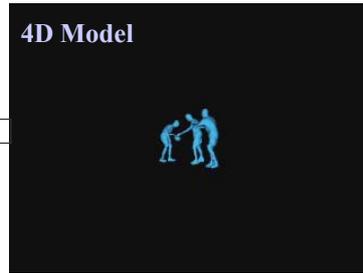


A virtual video from completely arbitrary view points can be synthesized from the 4D description, including "placing" the event in a "new" environment, like a synthetic gym.



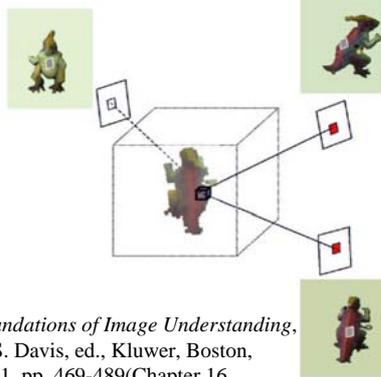
Example:
3-Man Basketball

(These are movies.)



Voxel Coloring/Space Curving

[Seitz and Dyer 97]

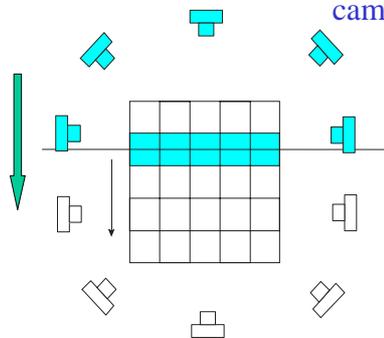


Foundations of Image Understanding,
L. S. Davis, ed., Kluwer, Boston,
2001, pp. 469-489(Chapter 16,
VOLUMETRIC SCENE
RECONSTRUCTION
FROM MULTIPLE VIEWS/Charles
R. Dyer)

Checking Photo-Consistency
of each voxel

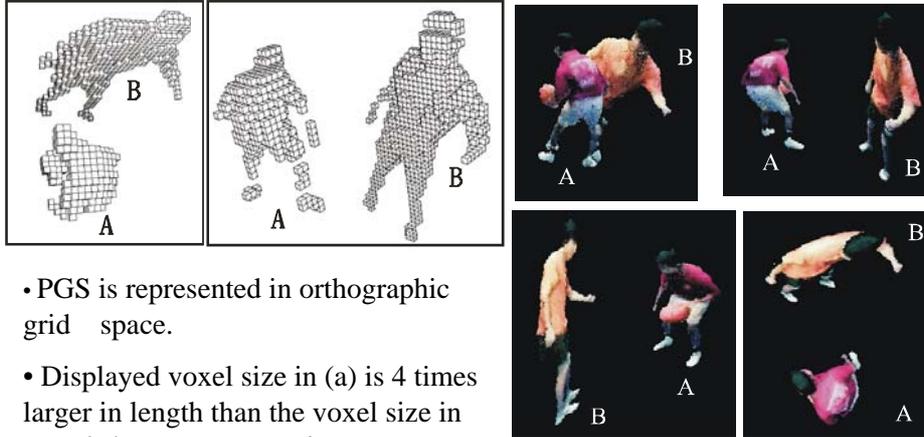
If consistent, the voxel should be
on the object surface

Viewing
cameras



Shape Modeling and Rendering via Voxel Coloring in Projective Grid Space

[Saito and Kanade 99]

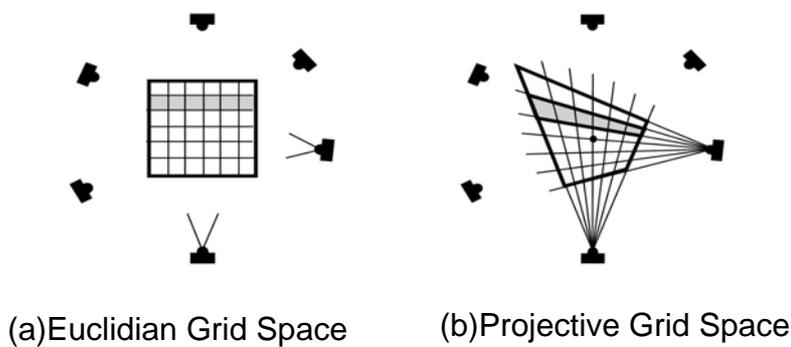


- PGS is represented in orthographic grid space.
- Displayed voxel size in (a) is 4 times larger in length than the voxel size in actual shape reconstruction.

Projective Grid Space by Weak Calibration

H. Saito, T. Kanade, Proc. CVPR'99, Vol.2, pp.49-54, 1999.

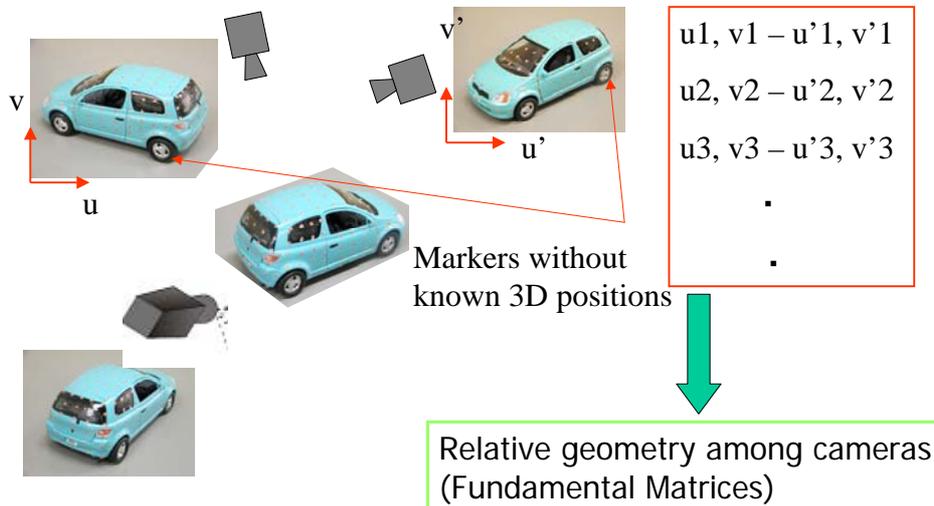
- Euclid Reconstruction (3D Space is defined independently from cameras)
→ **Artificial Maker with Known 3D Position**
- Projective Reconstruction (3D Space is defined dependently on cameras)
→ **Natural Maker without 3D Position**



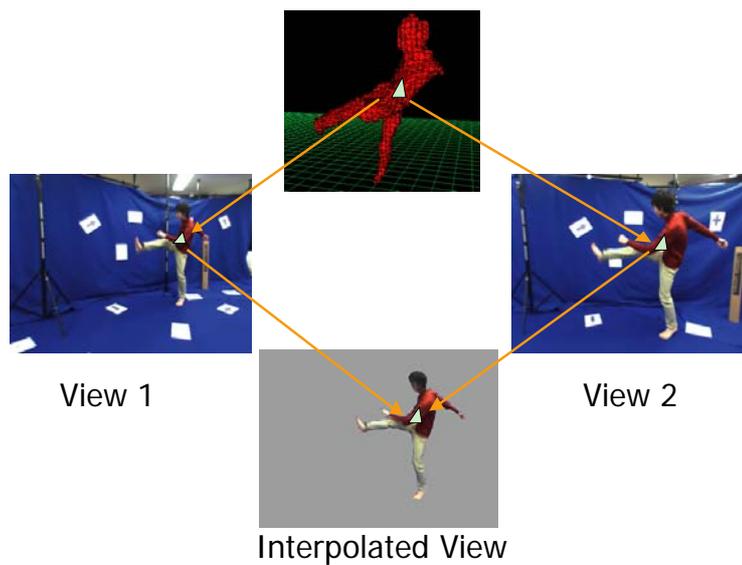
(a) Euclidian Grid Space

(b) Projective Grid Space

Weak Calibration



View Interpolation via 3D Model in PGS



Hand-Held Moving Multiple Cameras with Two Fixed Base-Cameras



Fixed Base Camera 1



Fixed Base Camera 2



Moving Camera A



Moving Camera B

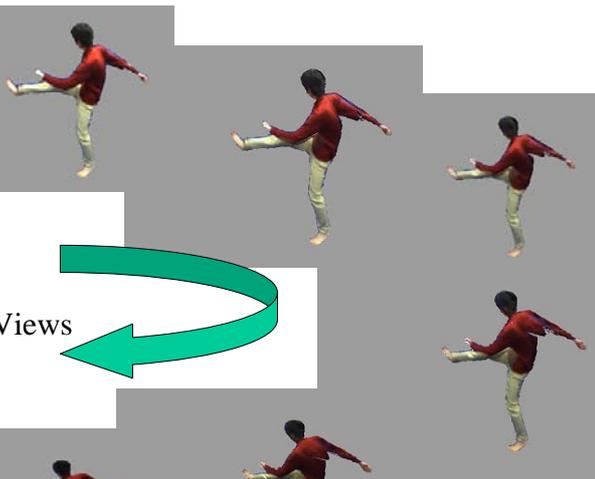


Moving Camera C

Moving by hand for tracking the object



Real View



Synthesized Intermediate Views



Real View

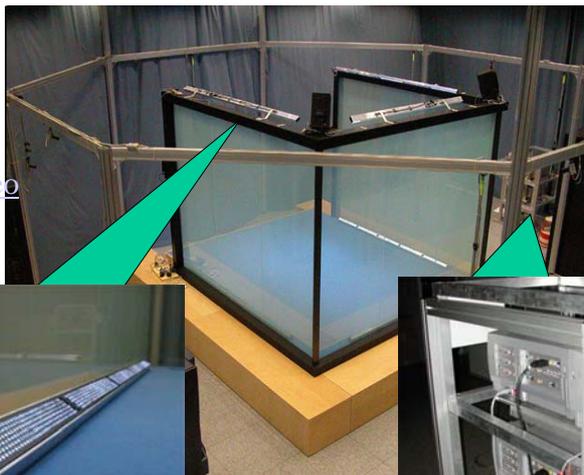


Intermediate image sequence of 5 cameras

blue-c Project (ETH Zurich)[Gross03]

<http://blue-c.ethz.ch/>

[Demo-video](#)



Rendering via Pixel Transfer

Pixel position of input image is transferred for synthesizing new viewpoint images.

Original position (x,y) \rightarrow Transferred position (u,v)

$$\begin{bmatrix} u \\ v \end{bmatrix} = f \begin{bmatrix} x \\ y \end{bmatrix}$$

Pixel transfer
Pixel position mapping

Affine Transform

$$\begin{bmatrix} u \\ v \end{bmatrix} = \begin{bmatrix} a & b \\ d & e \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} c \\ f \end{bmatrix}$$

$$\mathbf{u} = \mathbf{R}\mathbf{x} + \mathbf{t}$$

In the homogeneous coordinate representation

$$\begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$\tilde{\mathbf{u}} = \mathbf{H}\tilde{\mathbf{x}}$$

Homography

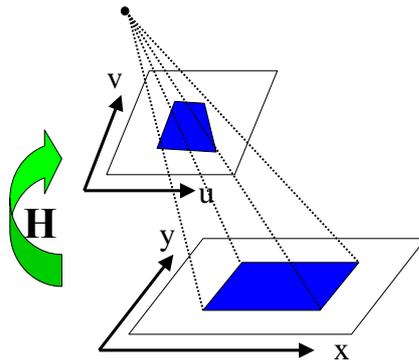
$$s \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

If $g=h=0$
then equal to affine transform

$$\tilde{\mathbf{u}} = \mathbf{H}\tilde{\mathbf{x}}$$

$$u = \frac{ax+by+c}{gx+hy+1}$$

$$v = \frac{dx+ey+f}{gx+hy+1}$$



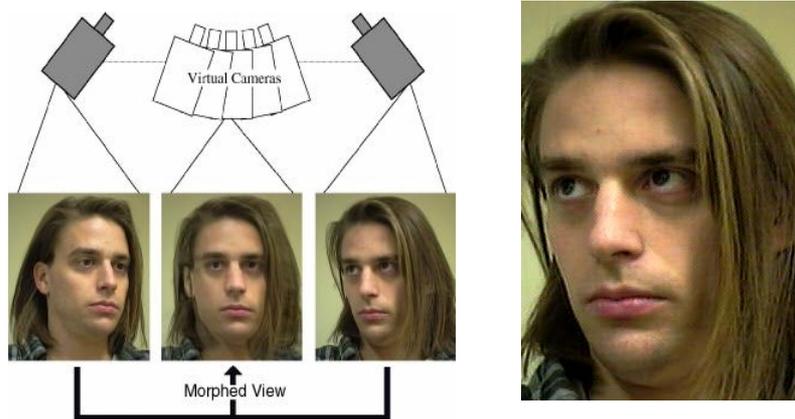
Free Viewpoint Observation



View Morphing

[Seitz and Dyer 96]

<http://www-2.cs.cmu.edu/~seitz/vmorph/vmorph.html>



Texture Mapping v.s. Pixel Transfer

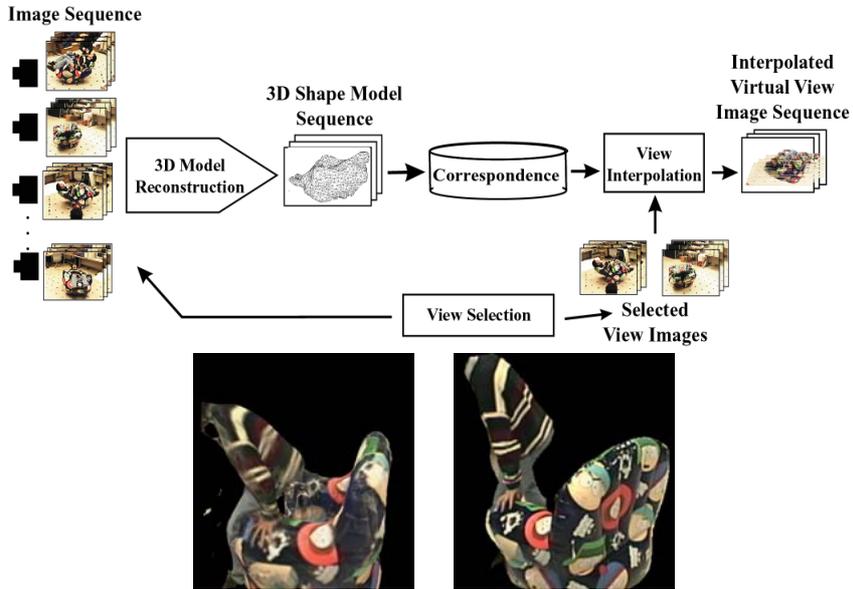


Texture Mapping

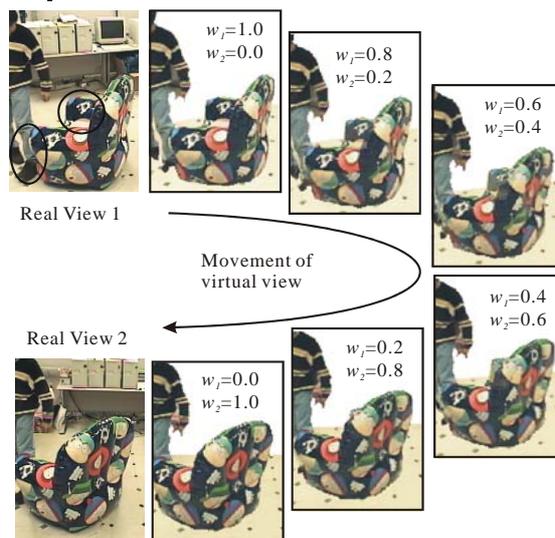


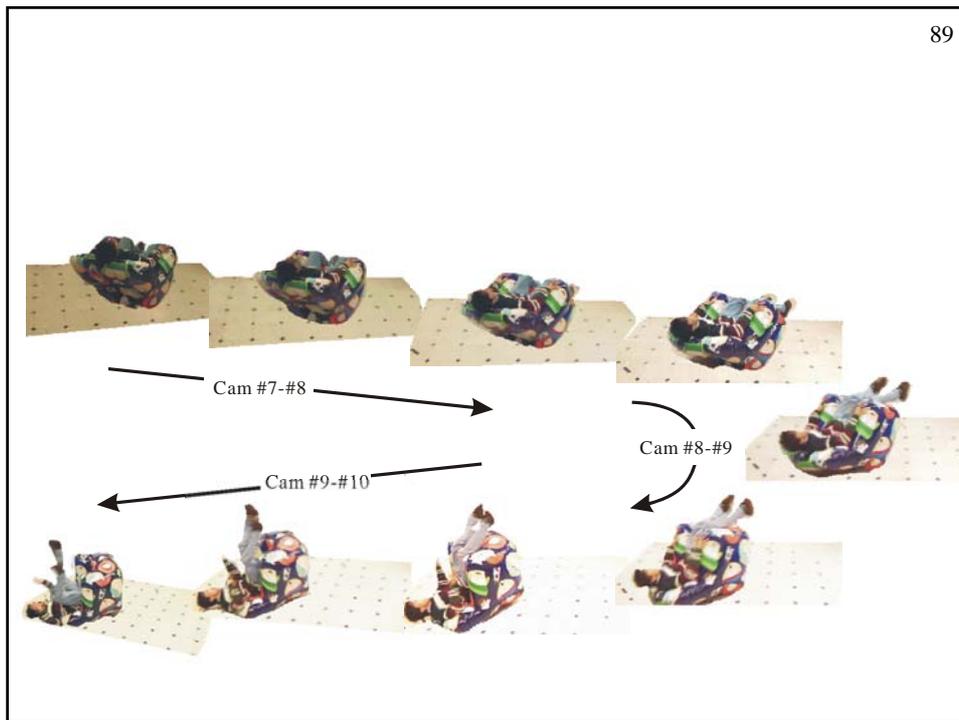
Pixel Transfer
(View Interpolation)

View Interpolation via 3D Model



Virtual View Images by Interpolation of Two Views

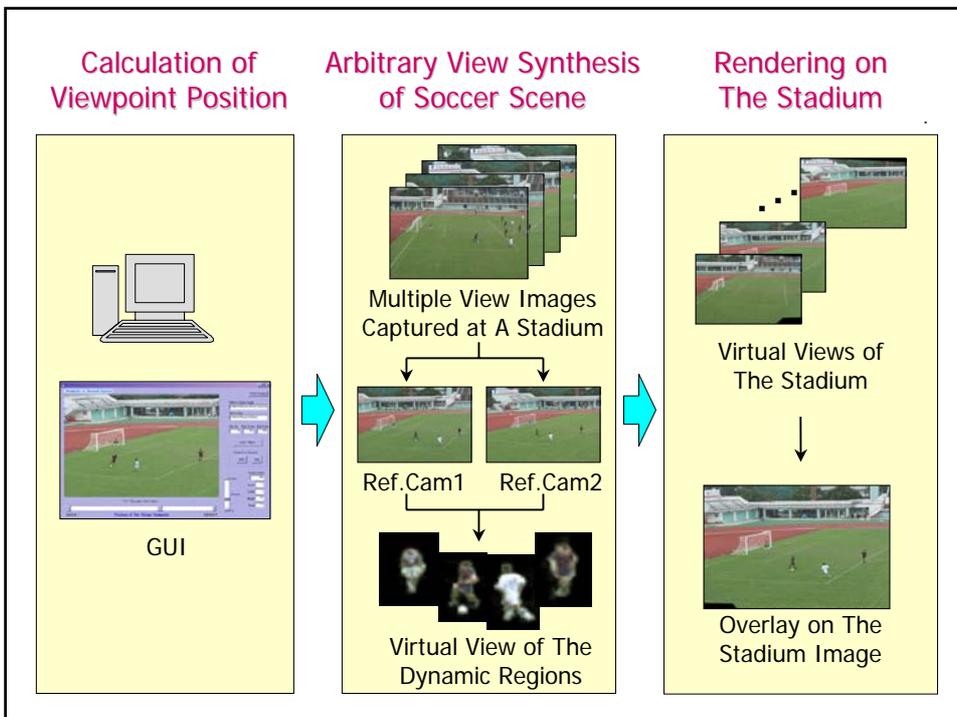
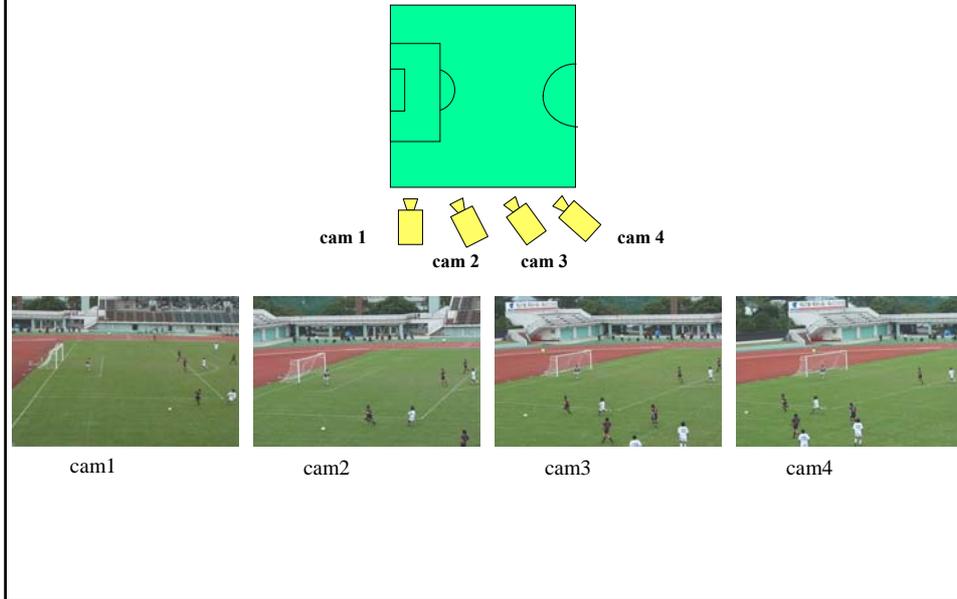




Free Viewpoint Synthesis for Soccer Scene

- Calibration of Multiple Cameras
 - Difficult to calibrate the cameras
 - Weak Calibration
- Shape Recovery Techniques
 - Almost impossible to recover 3D shapes
 - Simple Shape Representation
- Rendering Methods
 - View Interpolation/Morphing

For soccer scenes



View Synthesis for Dynamic Regions (1/2)

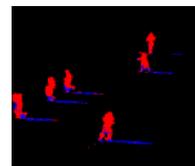
- **Detection**

- Subtraction of the background

- **Segmentation**

- Player/ball regions
- Shadow regions

- • Color information
HSI transform
- Geometric information
Homography transform



■ : Player/ball regions
■ : Shadow regions

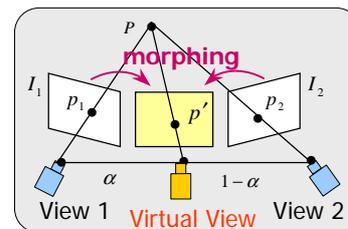
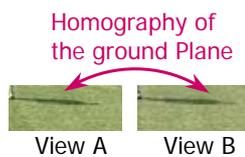
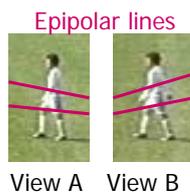
View Synthesis for Dynamic Regions (2/2)

- **Player Regions**

- Region Correspondence by Homography
- Pixel Correspondence by F-Matrix
- Morphing

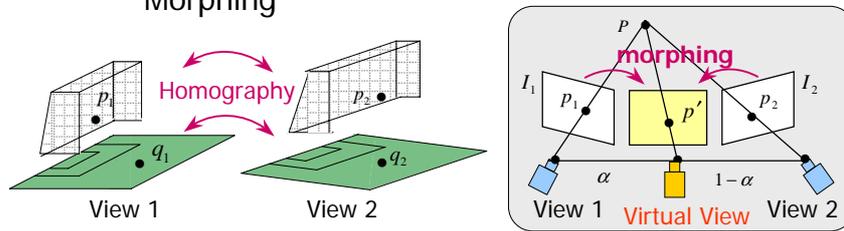
- **Shadow Regions**

- Pixel Correspondence by Homography
- Morphing



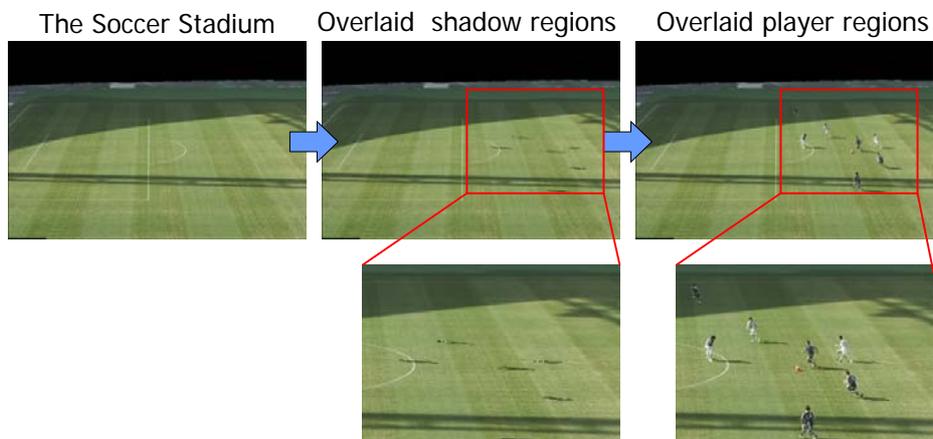
View Synthesis for Soccer Stadium

- **Background Region**
: approximated to plane at infinity
➔ Image mosaicking
- **Field Regions**
: approximated to planes
➔ Pixel correspondence by Homography
Morphing



Soccer Scene Representation

- Superimposing dynamic regions on the soccer stadium.



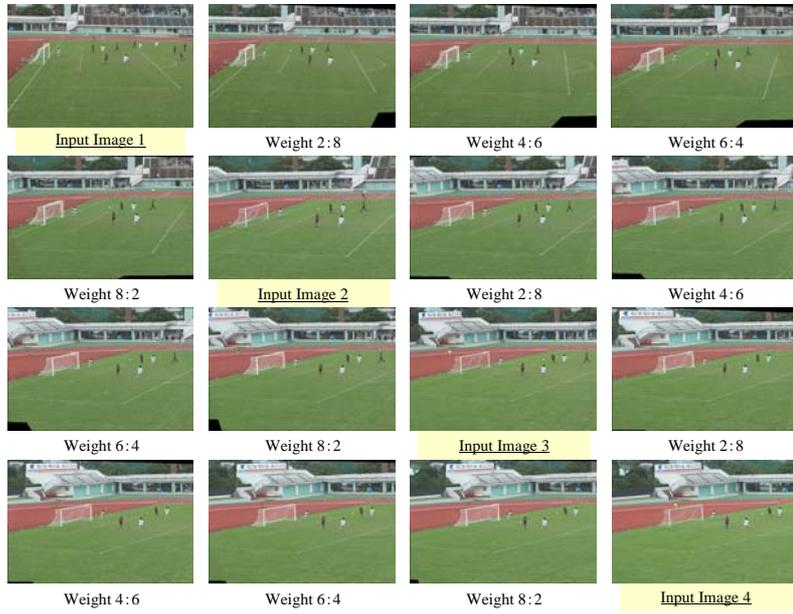
Virtual Viewpoint Visual Effect

— like “The Matrix” —



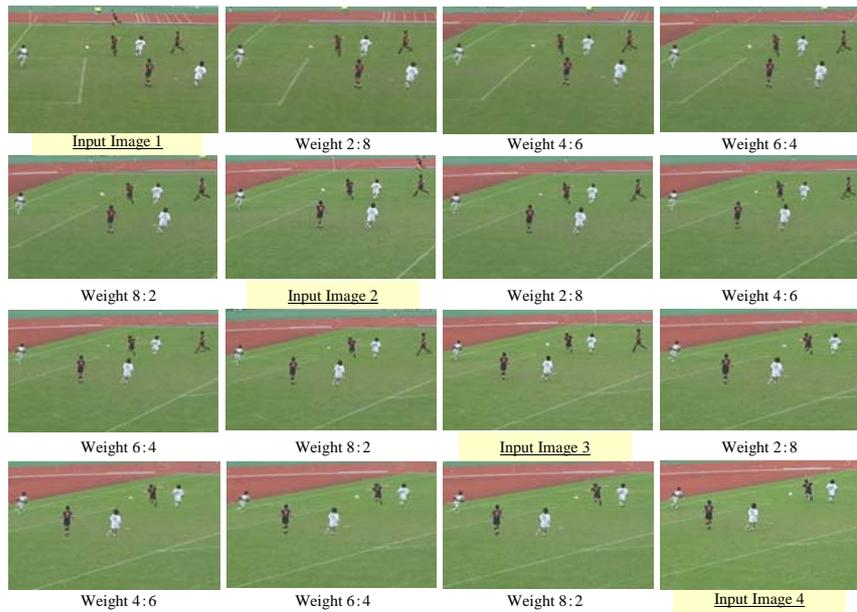
Intermediate Viewpoint Images

99



Intermediate Viewpoint Images (Magnified)

100



Comparison



Virtual Camera (Cam 2-4 Weight 5:5)

Real Camera (Cam 3)

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Input Video



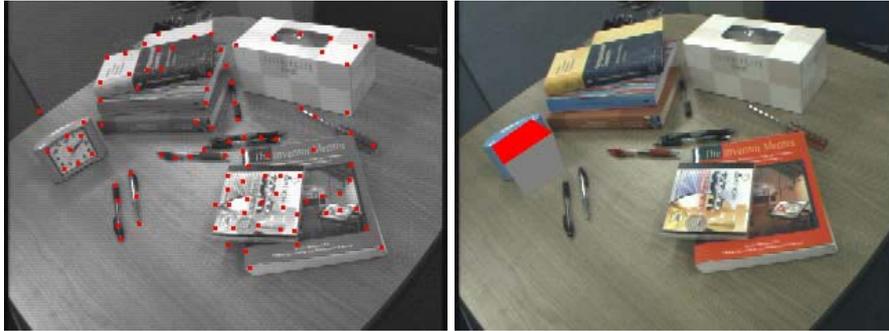
Synthesized Video
At Player's Viewpoint

Registration

Registration for AR/MR

- Feature Tracking is Key Technology.
- Estimate Motion of Camera for Registration.

Feature point based registration



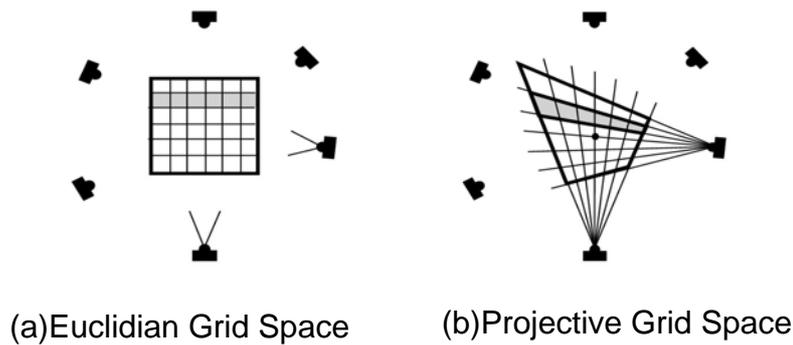
Line-segment Based Registration



Projective Grid Space by Weak Calibration ¹⁰⁷

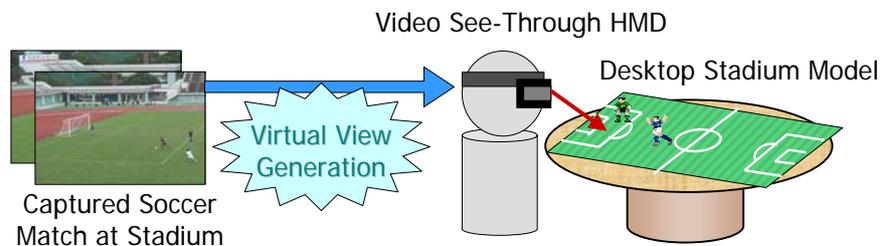
H. Saito, T. Kanade, Proc. CVPR'99, Vol.2, pp.49-54, 1999.

- Euclid Reconstruction (3D Space is defined independently from cameras)
→ **Artificial Maker with Known 3D Position**
- Projective Reconstruction (3D Space is defined dependently on cameras)
→ **Natural Maker without 3D Position**



Example of Image Based Registration - Immersive Observation System - ¹⁰⁸

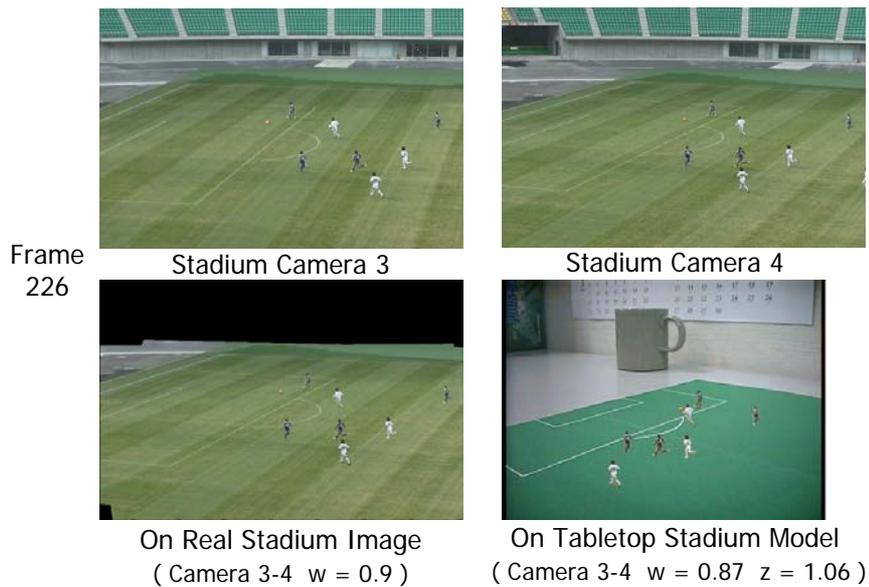
User sees a **desktop stadium model** in the real world with **video see-through HMD** and observes dynamic objects of soccer scene overlaid onto the display.



Result 1



Result 2



Immersive Observation System



Free Viewpoint Observation on the Desktop Stadium Mode with HMD



Stadium Model Captured by HMD Camera

Result

Arbitrary View Observation with HMD



Overlaid Soccer Scene on Tabletop Stadium Model

Example of Image Based Registration

Texture Overlay onto Deformable Surface Using HMD

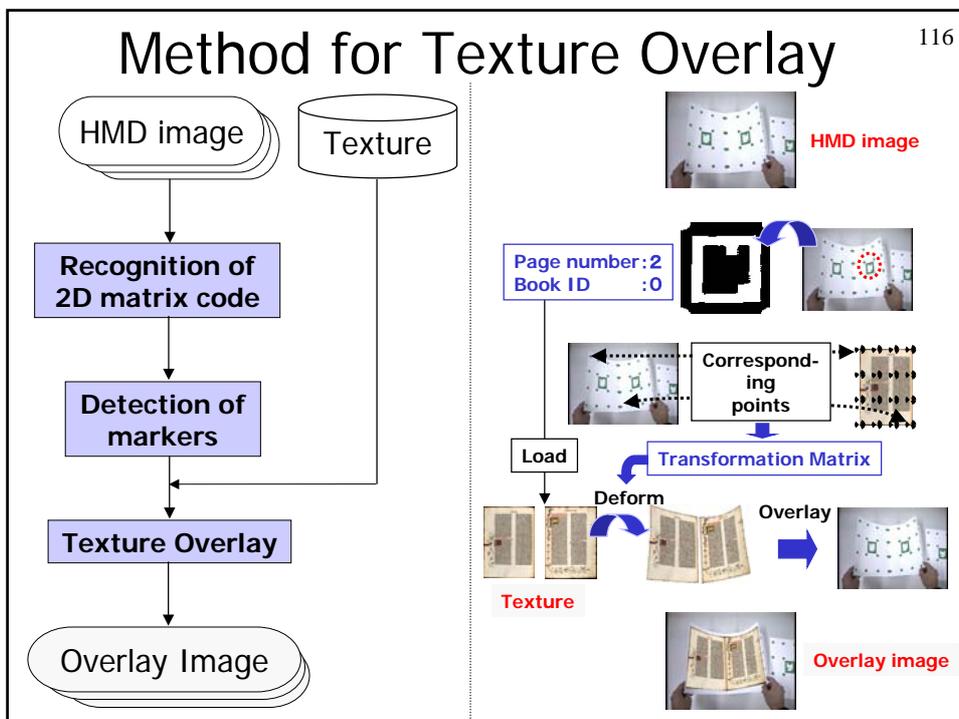
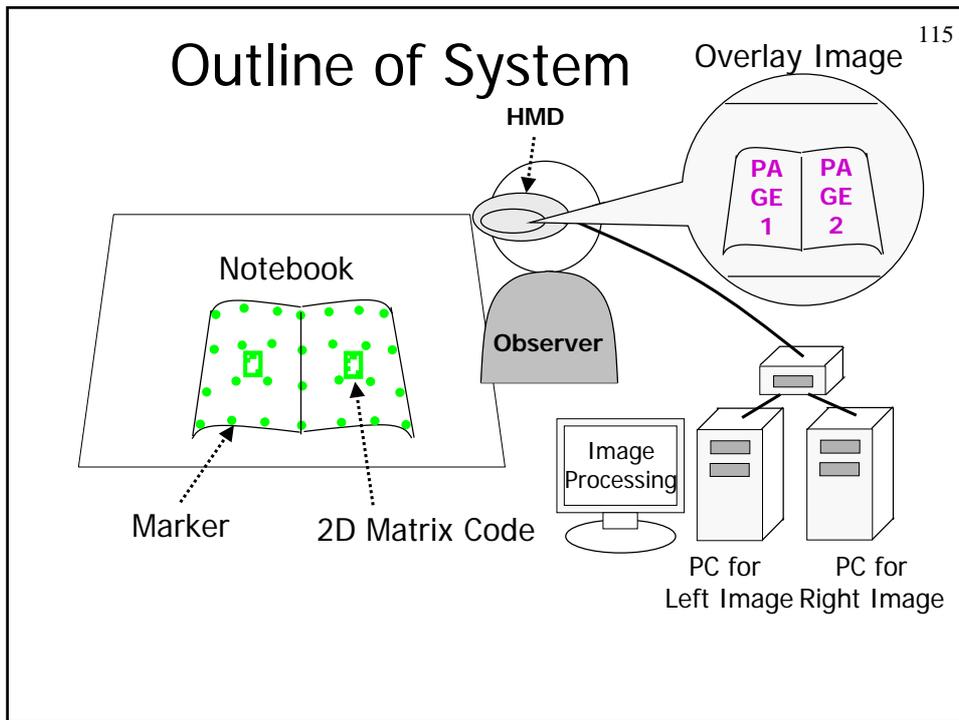
Purpose

Our propose is to overlay textures onto a deformable surface of an object in real time using a video see-through HMD.



Observer feels as if he was reading a real book.

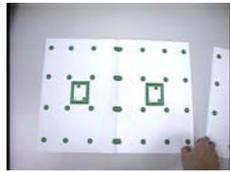




Implementation

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Input images : 640×480 pixels



HMD image



Appearance of experiment

HMD



Texture images : 350×500 pixels



book0, page1



book0, page2



book1, page3



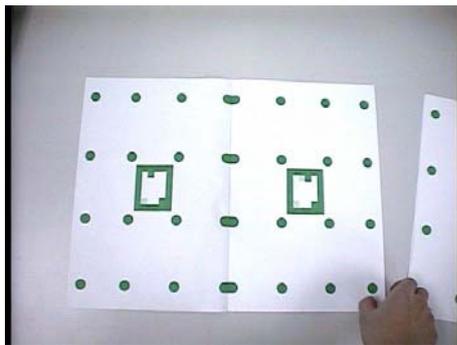
book1, page4

the Gutenberg Bible

the Conrad Gesner's Thierbuch

Result 1

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Original image



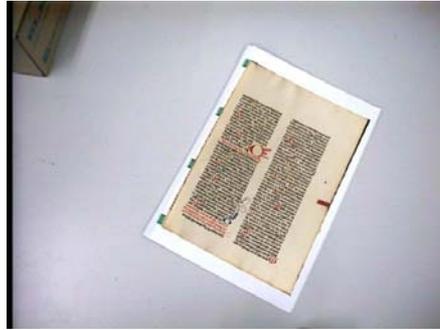
Overlay image

Result 2

A case that a book is turned upside down.



Overlay image 1



Overlay image 2

Result 3

A case that we turn a page.



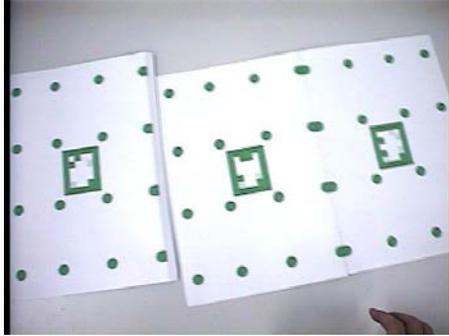
Page 1,2



Page 3,4

Result 4

A case that we see multiple books.



Original image



Overlay image



These results(2 ~ 4) shows that 2D matrix code is recognized correctly.

Result 5



Overlay images generated by the system

Conclusion

- Image/Video-based modeling/rendering, and registration for virtual reality application are introduced.
 - Camera geometry for capturing images
 - Modeling and rendering from image sequence, multiple cameras, reflectance analysis
 - Application of modeling and rendering to sporting scene
 - Application of image-based registration for AR/MR